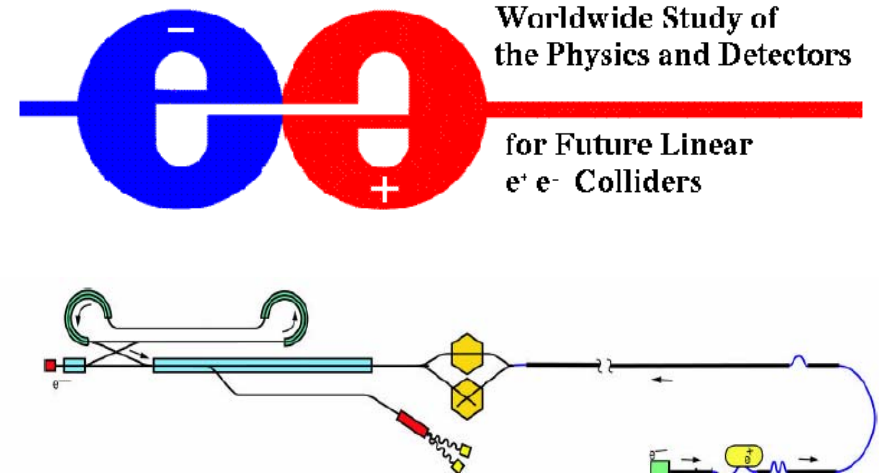
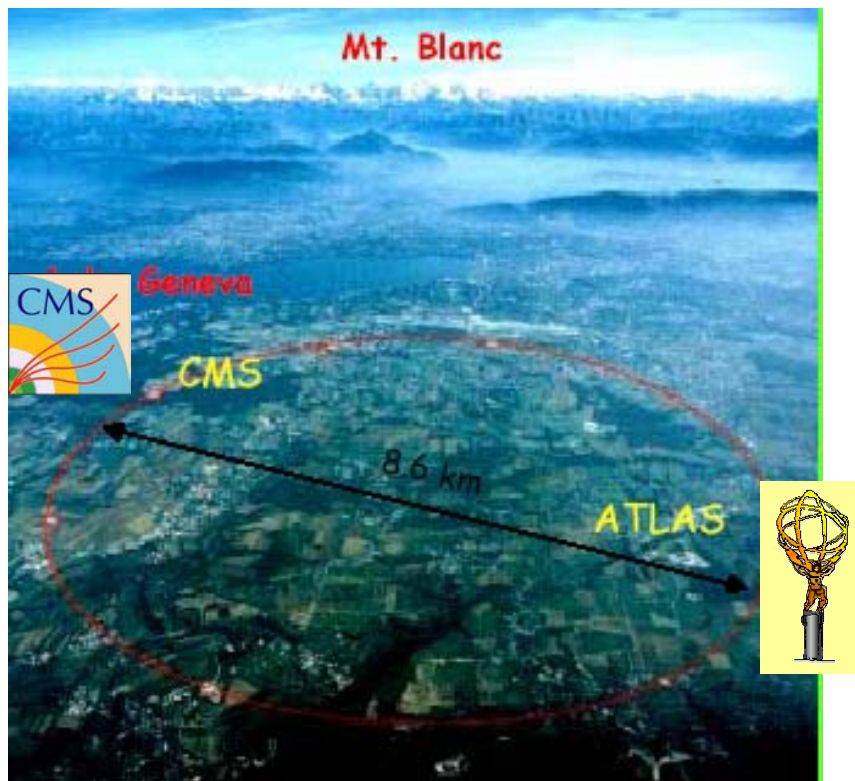


# Interplay Between the LHC and a Linear Collider

Albert De Roeck CERN  
Ecole de Gif 2004

Le Future de la Physique des Hautes Energies



# Contents

- Introduction:  $LHC \leftrightarrow LC$
- Examples of complementarity
  - Supersymmetry
  - Higgs
  - $Z'$  bosons
  - Extra dimensions
- Conclusion

# High Energy Frontier in HEP

## Next projects on the HEP roadmap

- **Large Hadron Collider LHC at CERN** → G. Unal
  - Approved, budget in place and under construction
  - Expected turn on in middle of 2007
- **Linear Collider (LC) ?** → H. Videau
  - Strong world-wide effort to start construction around 2009/2010, if approved and budget established
  - Expected turn on 2015(+)
  - Study groups in Europe, Americas and Asia (+World Wide Study)
- **Physics case for both machines separately is well established**
- **In Europe: up to LHC/LC study little contact between - experimental- the two communities (→"miss understandings"...) ⇒ Initiative to form a LHC/LC common study group in 2002**

# The LHC/LC study group

Aim of the LHC/LC Study group: investigate how the analyses at the LHC could profit from results obtained at the LC and vice versa - maybe even affect LHC running or triggers --

- Started in summer 2002 as a world wide effort
- Collaborative effort of the LHC and linear collider community.
- Study group which has been officially recognized by international linear collider steering committee (ILCSC)
- Current about 190 (interested) working group members from ATLAS, CMS, LC working groups + Tevatron contact person
- Working group coordinators: R. Godbole, G. Weiglein
- Web page `www.ippp.dur.ac.uk/~georg/lhc1c`
- First document with results is being finalized

# LHC/LC study group

## LHC / LC Study Group Working Document

ALL AUTHORS

Expect to finalize by fall 2004

<sup>1</sup> Institute 1

<sup>2</sup> Institute 2

### Abstract

The LHC / LC Study Group investigates the possible interplay between the LHC and a future  $e^+e^-$  Linear Collider in testing the Standard Model and in searches for new physics. It is studied in particular to what extent analyses carried out at one of the machines can profit from results obtained at the other machine. Mutual benefits can occur both at the level of a combined interpretation of Hadron Collider and Linear Collider data and at the level of combined analyses of the data, where results obtained at one machine can directly influence the way analyses are carried out at the other machine. Topics under study comprise the physics of weak and strong electroweak symmetry breaking, Supersymmetric models, new gauge theories, models with extra dimensions, and electroweak and QCD precision physics. The present report summarizes the status of the work that has been carried out within the LHC / LC Study Group so far. Possible topics for future studies are outlined.

Contains work discussed at ~ 5 meetings, in particular around/during Les Houches 2003 (May 2003)



- ⇒ Over 500 Pages already !?!
- ⇒ Mostly comparison studies between the two machines
- But a number of true complementarity studies...several are still ongoing
- ⇒ Not the final word

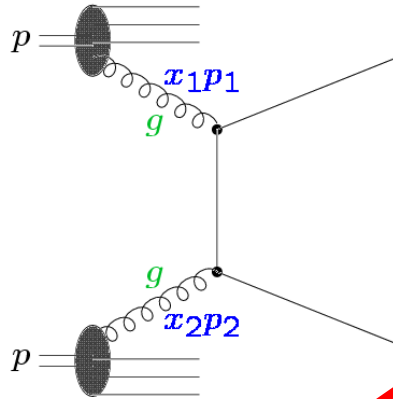
Will give several examples in the following

# LHC/LC studies

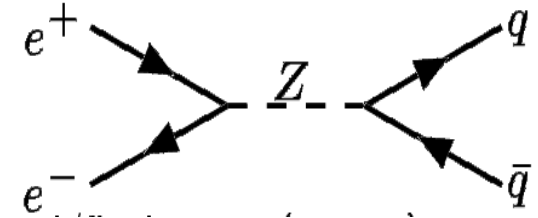
- Electroweak Symmetry breaking (weakly)  
H. Haber, R. Godbole, G. Weiglein, ADR (\*)
- Strong Electroweak Symmetry breaking  
T. Barklow, K. Moenig
- Supersymmetric Models  
K. Desch, K. Kawagoe, M. Nijori, F. Paige, G. Pollesello
- New Gauge Theories  
S. Riemann
- Models with Extra Dimensions  
J. Hewett
- Exotics  
J. Gunion
- Electroweak and QCD precision tests  
E. Boos, S. Heinemeyer, J. Stirling, ADR

(\*) = main chapter editors/organizers

# LHC/LC



Different characteristics  
of the two machines  
⇒ Different capabilities  
& virtues



LHC pp collisions  $\sqrt{s}$  = at 14 TeV

⇒ Strong point: larger mass reach  
for direct discoveries

- Kinematics: can use conservation of p
- Composite nature of colliding protons  
⇒ underlying event
- $\sqrt{s}$  of the hard interaction not fixed
- Strongly interacting particles  
⇒ huge QCD cross sec. (background)

$e^+e^-$  collisions at  $\sqrt{s}$  = 0.5-1.0 TeV

⇒ Strong point: high precision  
physics

- Kinematics: mom. conservation  
used to analyze the decays,...
- Well defined initial state,  
beam polarization,  $\sqrt{s}$ ,...
- Backgrounds smaller than LHC
- Options:  $\gamma\gamma$ ,  $e\gamma$ ,  $e-e^-$  colliders.

# The LHC/LC study

- Physics case well established for the LHC and LC
  - Not the aim to see who is better (always tempting of course...)
  - One of the purposes is to make both communities aware when designing there analyses on what kind of additional information they might get when a LC kicks in
- Interplay between LHC and a LC can happen at different levels
  - Combined interpretation of LHC/LC data
    - ⇒ In particular to reduce possible model dependencies
  - $$\text{LHC} \oplus \text{LC} > \text{LHC} + \text{LC}$$
  - Combined analyses of LHC and LC (simultaneous running)
  - $$\text{LHC} \otimes \text{LC} > \text{LHC} \oplus \text{LC}$$
- If a LC gets into operation in time, could even influence detector/trigger choices at LHC upgrades (time-of-flight, softer scales, particle ID,...)
  - ⇒ Can help to make the case for concurrent running of LHC and a LC

# Linear Collider Time Scales

R. Heuer LCWS04

## ILCSC Road Map

2004 technology recommendation (confirmed by ITRP)

Establish Global Design Initiative / Effort (GDI/E)

2005 CDR for Collider (incl. first cost estimate)

2007 TDR for Collider

2008 site selection

2009/2010 construction could start (if budget approved)



First collisions in 2015?

Certainly a challenge

LC the first real "global machine" in HEP?

# A LC Collider

## International LC scope document

- 500 GeV, and upgradeable to  $\sim 1$  TeV,
- 500 fb<sup>-1</sup> in 4 years at 500 GeV
- 2 interaction regions,
- 80% electron polarization
- Energy flexibility between  $\sqrt{s} = 90\text{-}500$  GeV
- Future: possibility of  $\gamma\gamma$ ,  $e^-e^-$ ,  $e^+$  polarization, Giga-Z

$\Rightarrow$  TeV  $e^+e^-$  Linear Collider

# LHC Status/plans

- Date for first beams/collisions:  $\Rightarrow$  **Spring 2007**
- Initial physics run starts in summer/fall 2007
  - $\Rightarrow$  collect  $\sim 10 \text{ fb}^{-1} / \text{exp}$  ( $2 \cdot 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$ ) by early 2008
- Depending on the evolution of the machine...
  - $\Rightarrow$  collect  $200\text{-}300 \text{ fb}^{-1} / \text{exp}$  ( $3.4\text{-}10 \cdot 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$ ) in 5-6 years time

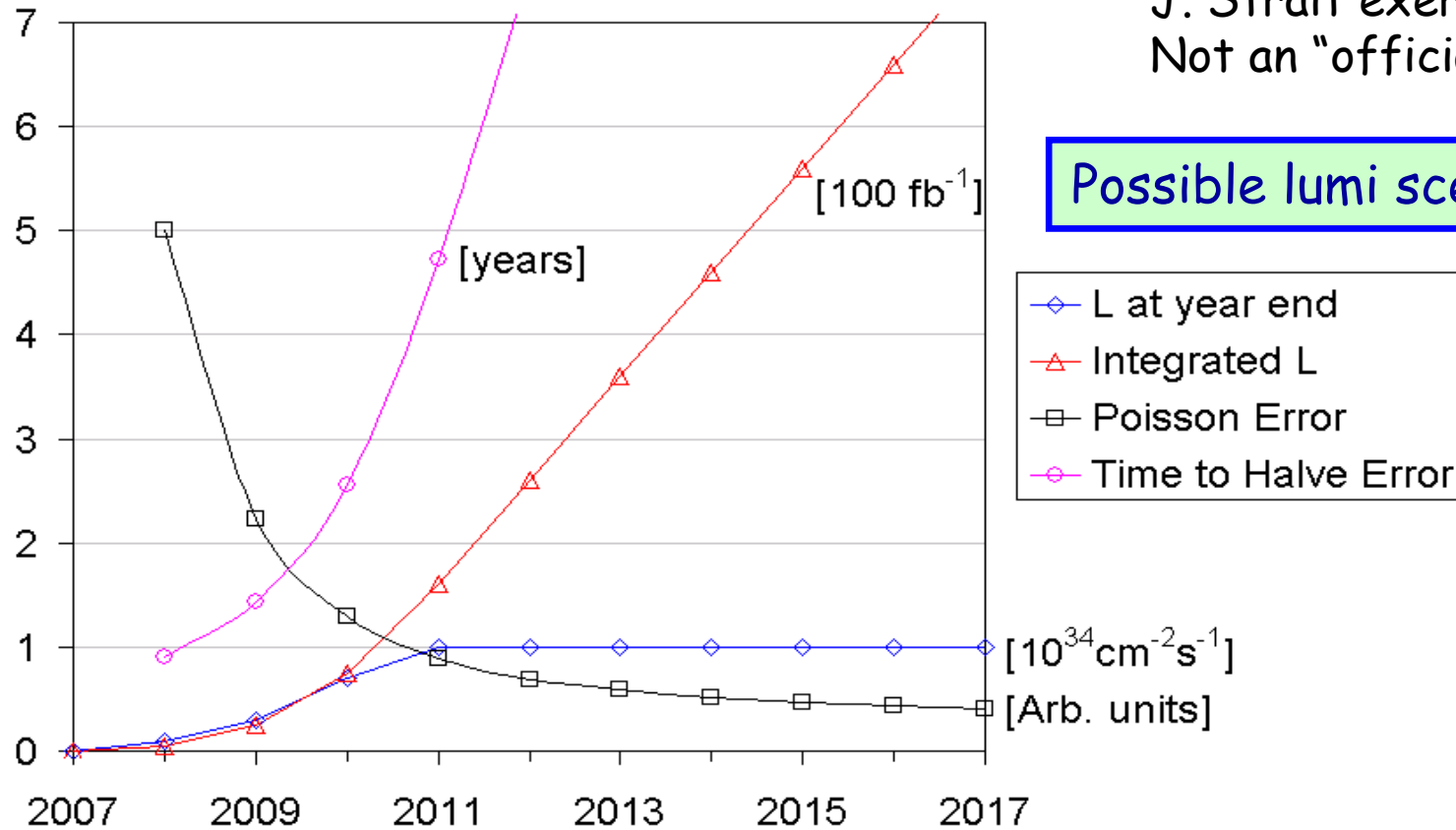
Already time to think of upgrading the machine

Two options presently discussed/studied

- Higher luminosity  $\sim 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$  (SLHC)
  - Needs changes in machine and particularly in the detectors
    - $\Rightarrow$  Start change to SLHC mode some time 2013-2016
    - $\Rightarrow$  Collect  $\sim 3000 \text{ fb}^{-1} / \text{experiment}$  in 3-4 years data taking.
- Higher energy?
  - LHC can reach  $\sqrt{s} = 15 \text{ TeV}$  with present magnets (9T field)
  - $\sqrt{s}$  of 28 (25) TeV needs  $\sim 17$  (15) T magnets  $\Rightarrow$  R&D needed!

# Upgrades of the LHC

J. Strait exercise:  
Not an "official" LHC plot



If startup is as smooth as assumed here:  
⇒ Around 2013: simple continuation becomes less exciting  
⇒ Time for an upgrade?

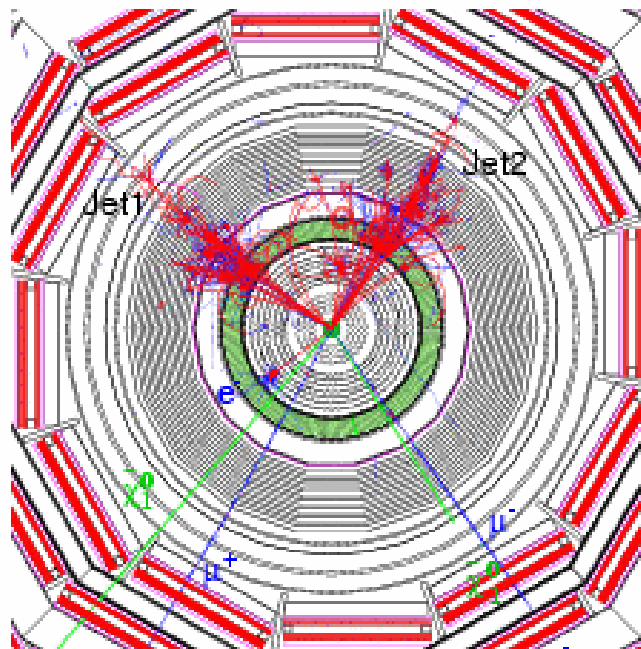
# By the Time the LC Turns on...

- The LHC luminosity upgrade complete or nearing completion
  - ⇒  $\sim 300 \text{ fb}^{-1}$ /experiment accumulated
  - ⇒ LHC luminosity =  $10^{35}/\text{cm}^{-2}\text{s}^{-1}$
- Physics is focused on
  - Improvements in determination of SM parameters  
(Higgs & gauge boson couplings)
  - Improvements of accuracy of new physics parameters  
(sparticle spectroscopy,  $\tan\beta$  measurements)
  - Extension of the high mass discovery reach
  - Extension of the sensitivity to rare processes  
(FCNC top decays, Higgs pair production...)

The hard stuff

Discovery Physics → Spectroscopy

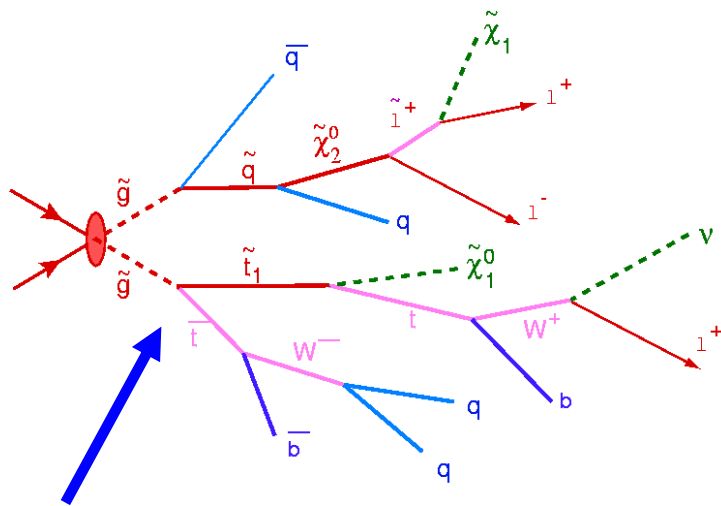
# 1. Supersymmetry



# Supersymmetry

Supersymmetry (SUSY) → assumes a new hidden symmetry between the bosons (particles with integer spin) and fermions (particles with half integer spin) to stabilize the Higgs mass up to the Planck scale

⇒ Lots of new particles (**squarks, sleptons, ...**) predicted with masses in the range from 10's of GeV's up to several TeV range



3 isolated leptons  
+ 2 b-jets  
+ 4 jets  
+  $E_t^{\text{miss}}$

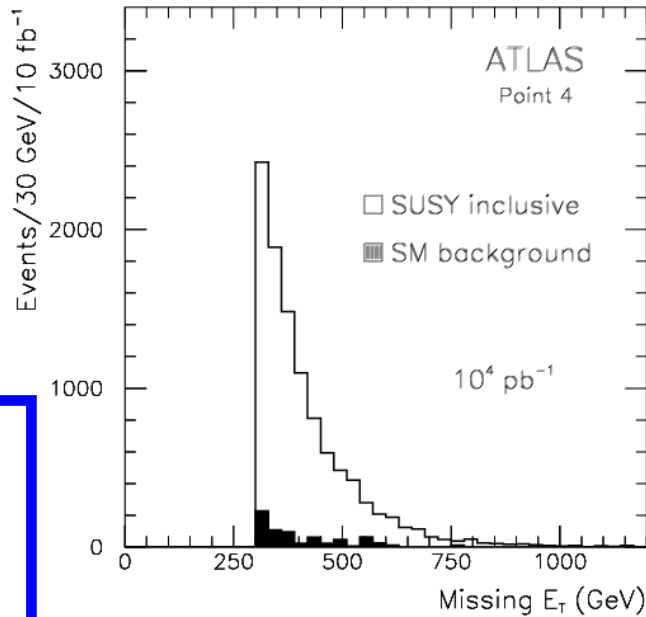
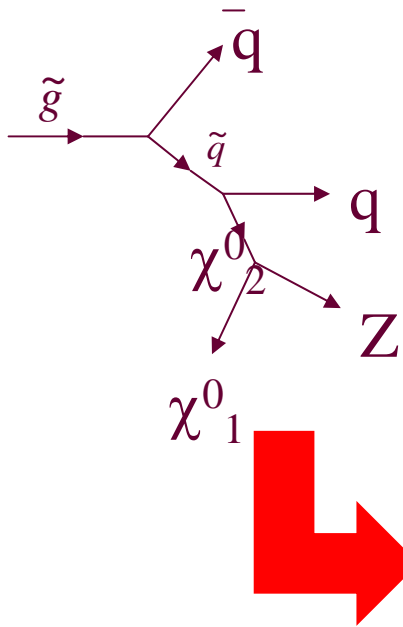
Should SUSY be realized, we have a lot to do

- Is it really SUSY?
- How is it realized?  
(particle content) MSSM NMSSM, ...
- How is it broken?  
Measure as many of the ~100 low energy parameters as possible  
Measure them precisely as possible  
→ Extrapolation to high scale

Lightest SUSY particle stable: dark matter candidate ?

# SUSY at the LHC

Discovery should be 'easy'  
for squark masses  $< \sim 2$  TeV



E.G. 900 GeV  
squarks  
 $E_{\text{miss}} > 300$  GeV  
+ 4 jets

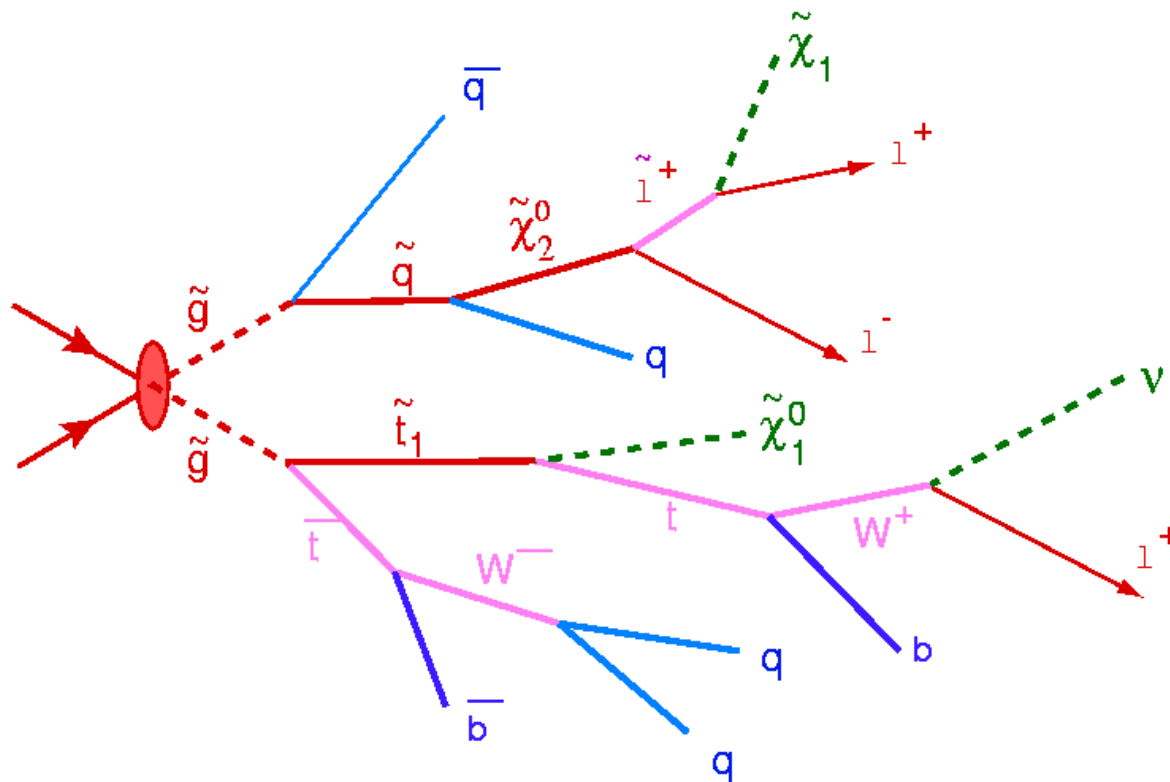


**DISCOVERY**



**SUSY SPECTROSCOPY?**

# SUSY at the LHC



- 3 isolated leptons
- + 2 b-jets
- + 4 jets
- +  $E_t^{\text{miss}}$

But exclusive reconstruction often difficult

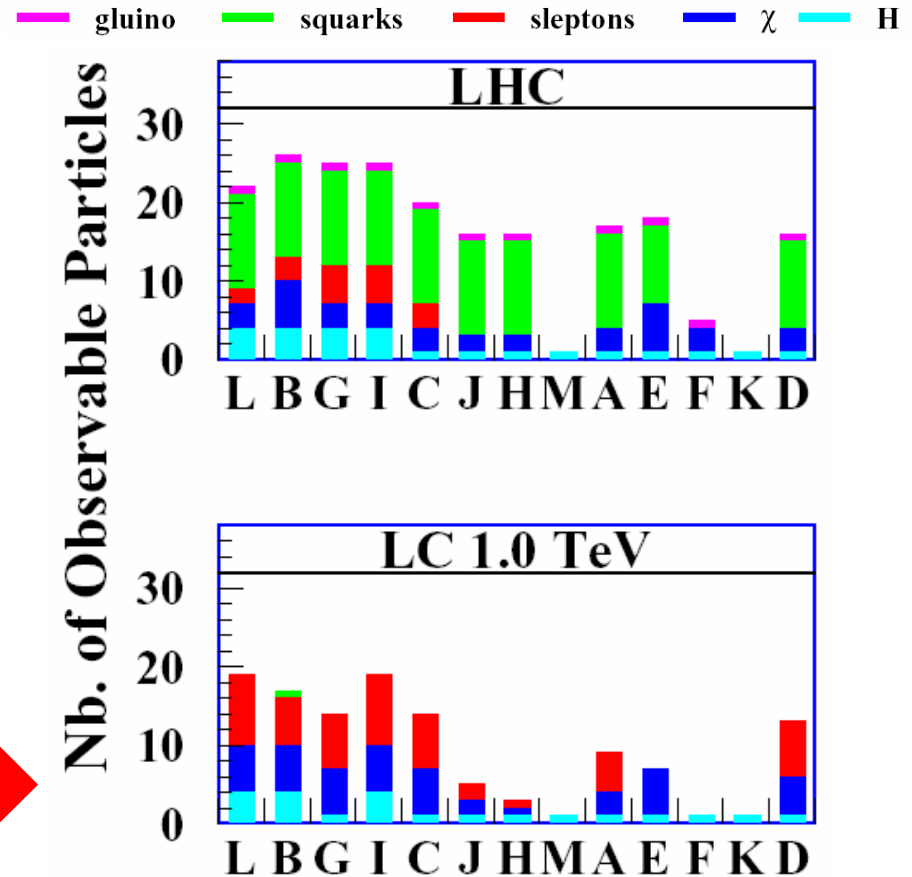
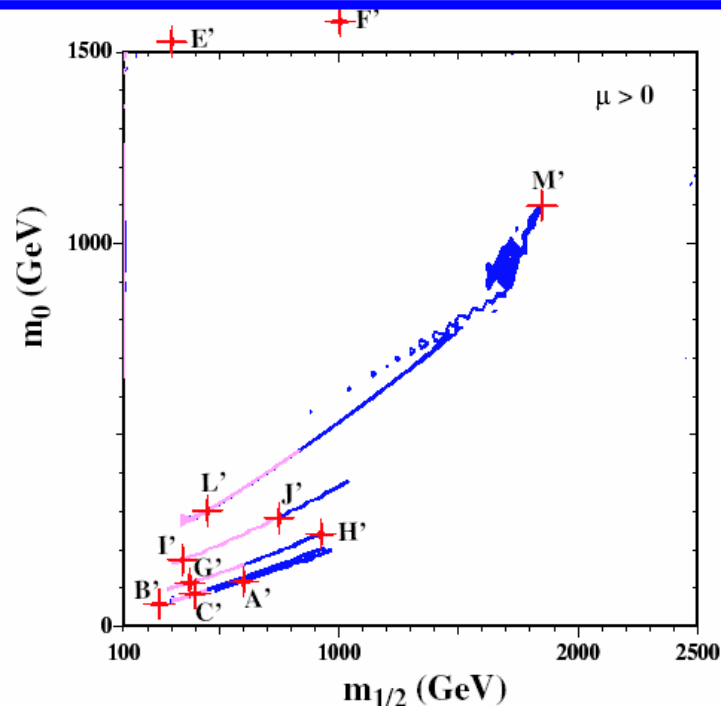
# Sparticle discoveries

- A number of SUSY (msugra) benchmark points to study LHC/LC sensitivity

(Battaglia, ADR, Ellis, Gianotti, Olive, Pape)

- Take into account direct searches at LEP and Tevatron, BR ( $b \rightarrow s\gamma$ ),  $g_\mu - 2$  (E821), Cosmology:  $0.09 \leq \Omega_\chi h^2 \leq 0.13$

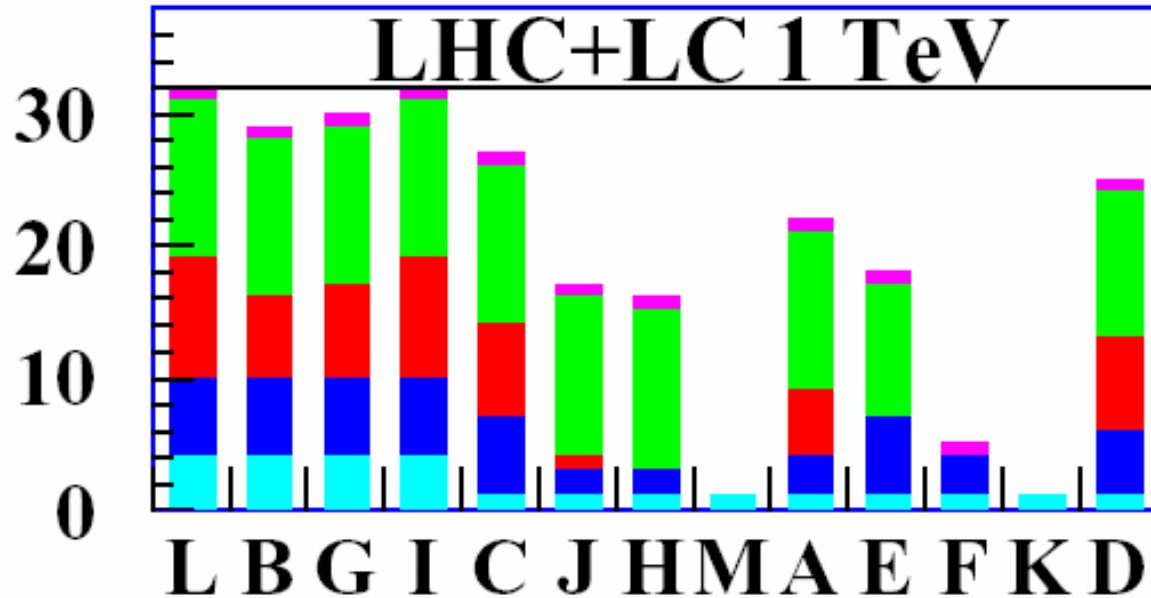
Allowed regions in the  $M_0$ - $M_{1/2}$  plane



Complementarity in sparticle reach  
 LHC: mostly squarks/gluinos  
 LC: mostly gauginos, sleptons

# LHC⊕LC

■ gluino   ■ squarks   ■ sleptons   ■  $\chi$    ■ H



For several of these scenarios (almost) all particles can be detected

Just an example... there are many more (also non-msugra) scenarios in use..

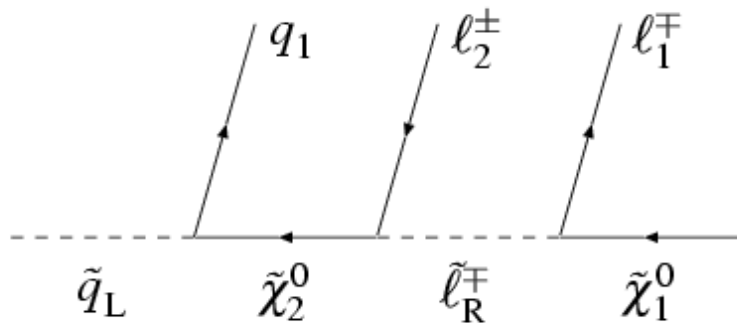
For the LHC/LC study: **Choose point B (SPS1a)**  
Favorable point for LHC/LC!! Maybe Nature will be less kind...

# 1. Measurement of Sparticle Masses

Gjelsten, Lytken, Miller, Osland, Polesello, Chiorboli, Tricomi, ADR

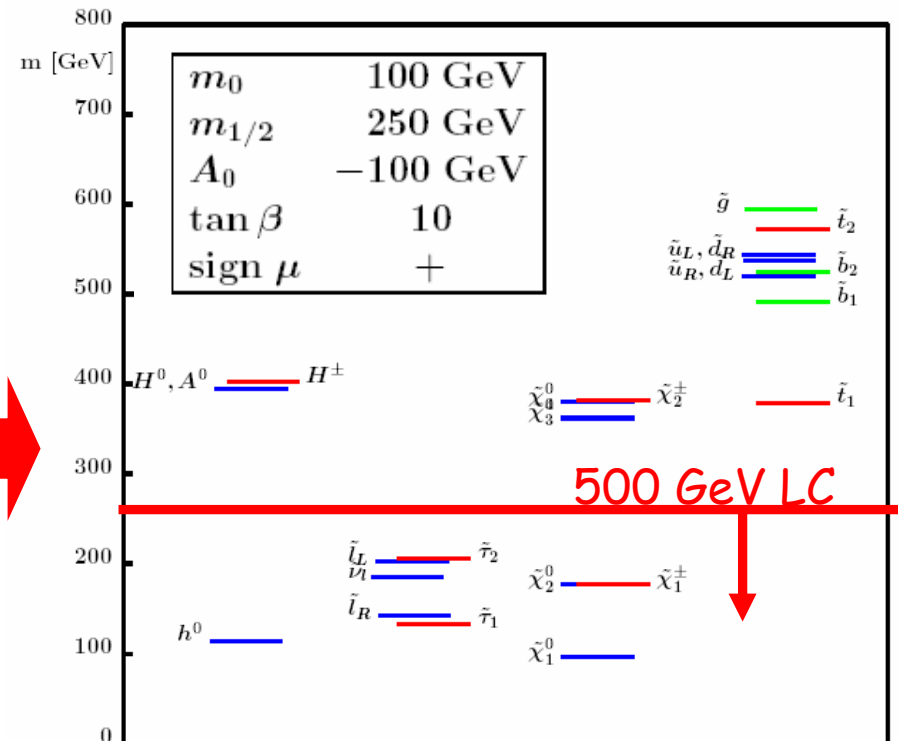
To understand SUSY breaking we will need to measure as many parameters as possible, e.g. sparticle masses

LHC: complicated by decay chains for squarks and gluons



Examples worked out for SPS1a (point B) in ATLAS/CMS

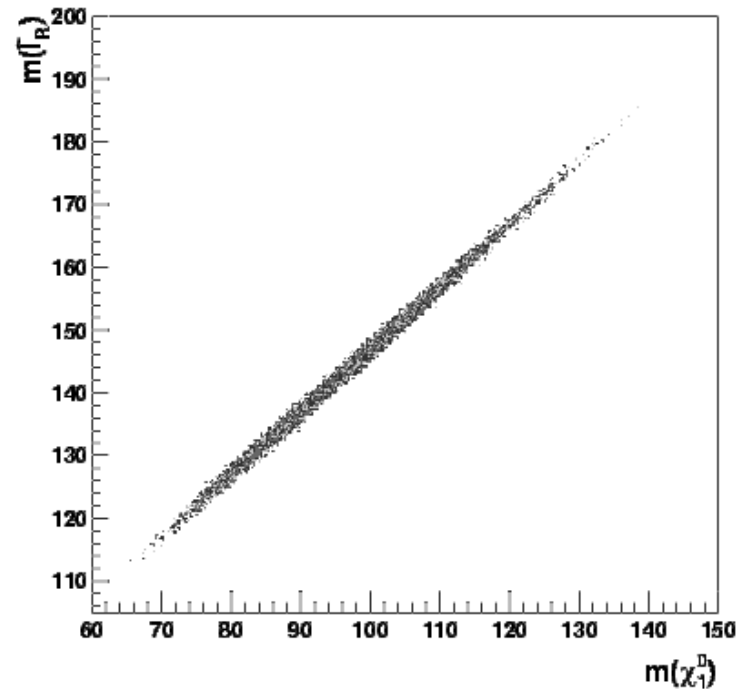
LHC will see all squarks, H,A and may see most gauginos





# Mass Correlations

Masses of the measured particles are strongly correlated with the mass of the lightest neutralino



However LHC can do better analyzing many edges simultaneously

... but correlations between masses will remain

# General "Edge" Analysis

Analyse many edges of distributions:

$$(m_{ll}^2)^{\text{edge}} = \frac{(m_{\tilde{\chi}_2^0}^2 - m_{\tilde{l}_R}^2)(m_{\tilde{l}_R}^2 - m_{\tilde{\chi}_1^0}^2)}{m_{\tilde{l}_R}^2}$$

$$(m_{qll}^2)^{\text{edge}} = \frac{(m_{\tilde{q}_L}^2 - m_{\tilde{\chi}_2^0}^2)(m_{\tilde{\chi}_2^0}^2 - m_{\tilde{\chi}_1^0}^2)}{m_{\tilde{\chi}_2^0}^2}$$

$$(m_{ql}^2)^{\text{edge}}_{\text{min}} = \frac{(m_{\tilde{q}_L}^2 - m_{\tilde{\chi}_2^0}^2)(m_{\tilde{\chi}_2^0}^2 - m_{\tilde{l}_R}^2)}{m_{\tilde{\chi}_2^0}^2}$$

$$(m_{ql}^2)^{\text{edge}}_{\text{max}} = \frac{(m_{\tilde{q}_L}^2 - m_{\tilde{\chi}_2^0}^2)(m_{\tilde{l}_R}^2 - m_{\tilde{\chi}_1^0}^2)}{m_{\tilde{l}_R}^2}$$

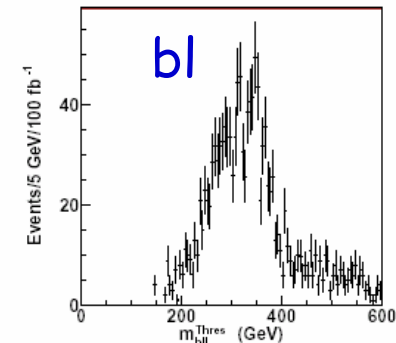
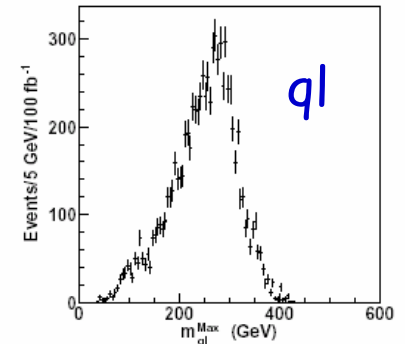
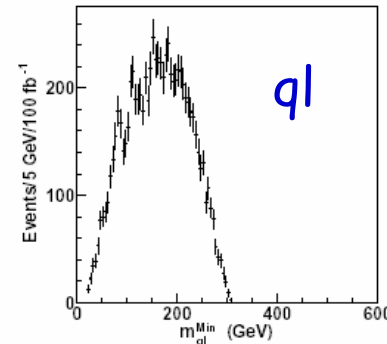
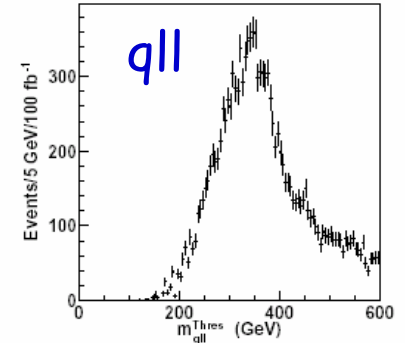
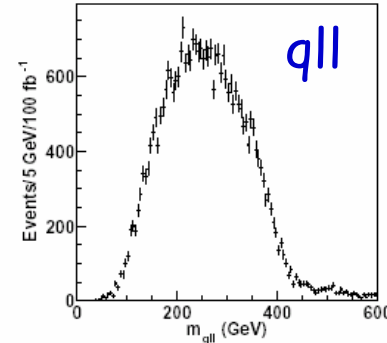
$$(m_{qll}^2)^{\text{thres}} = [(m_{\tilde{q}_L}^2 + m_{\tilde{\chi}_2^0}^2)(m_{\tilde{\chi}_2^0}^2 - m_{\tilde{l}_R}^2)(m_{\tilde{l}_R}^2 - m_{\tilde{\chi}_1^0}^2)$$

$$- (m_{\tilde{q}_L}^2 - m_{\tilde{\chi}_2^0}^2) \sqrt{(m_{\tilde{\chi}_2^0}^2 + m_{\tilde{l}_R}^2)^2 (m_{\tilde{l}_R}^2 + m_{\tilde{\chi}_1^0}^2)^2 - 16 m_{\tilde{\chi}_2^0}^2 m_{\tilde{l}_R}^4 m_{\tilde{\chi}_1^0}^2}$$

$$+ 2 m_{\tilde{l}_R}^2 (m_{\tilde{q}_L}^2 - m_{\tilde{\chi}_2^0}^2)(m_{\tilde{\chi}_2^0}^2 - m_{\tilde{\chi}_1^0}^2)] / (4 m_{\tilde{l}_R}^2 m_{\tilde{\chi}_2^0}^2)$$

Min,max refer to choice of lepton

SPS1a



Solve numerically equations  $\Rightarrow$  derive masses

# Extracted Edge Values

SPS1a 300 fb<sup>-1</sup>  
Includes 1% energy-scale systematics

Variable	Value (GeV)	Stat. (GeV)	Errors	
			Scale (GeV)	Total
$m_{\ell\ell}^{max}$	77.07	0.03	0.08	0.08
$m_{\ell\ell q}^{max}$	428.5	1.4	4.3	4.5
$m_{\ell q}^{low}$	300.3	0.9	3.0	3.1
$m_{\ell q}^{high}$	378.0	1.0	3.8	3.9
$m_{\ell\ell q}^{min}$	201.9	1.6	2.0	2.6
$m_{\ell\ell b}^{min}$	183.1	3.6	1.8	4.1
$m(\ell_L) - m(\tilde{\chi}_1^0)$	106.1	1.6	0.1	1.6
$m_{\ell\ell}^{max}(\tilde{\chi}_4^0)$	280.9	2.3	0.3	2.3
$m_{\tau\tau}^{max}$	80.6	5.0	0.8	5.1
$m(\tilde{g}) - 0.99 \times m(\tilde{\chi}_1^0)$	500.0	2.3	6.0	6.4
$m(\tilde{q}_R) - m(\tilde{\chi}_1^0)$	424.2	10.0	4.2	10.9
$m(\tilde{g}) - m(\tilde{b}_1)$	103.3	1.5	1.0	1.8
$m(\tilde{g}) - m(\tilde{b}_2)$	70.6	2.5	0.7	2.6

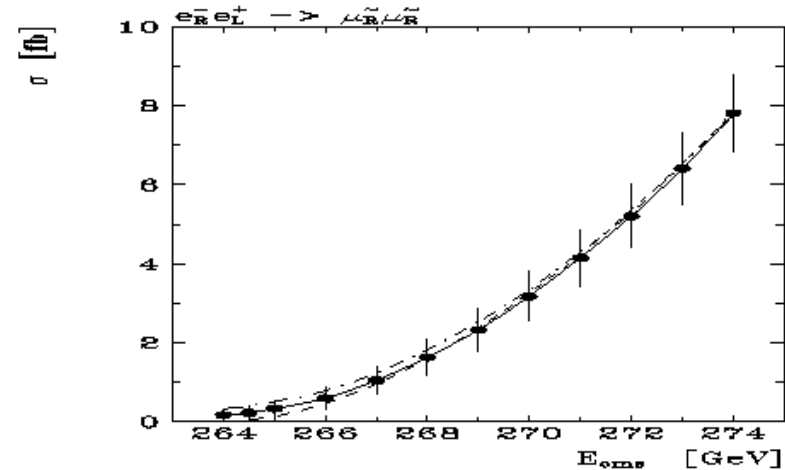
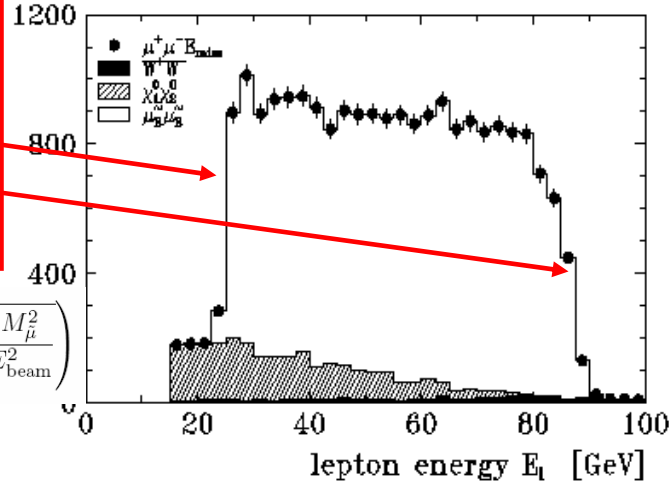
# Supersymmetry at a LC

Measure single muons

$\tilde{\mu}$  Threshold Scan

Kinematics:  
end-points allows  
to measure  
sparticle masses  
precisely

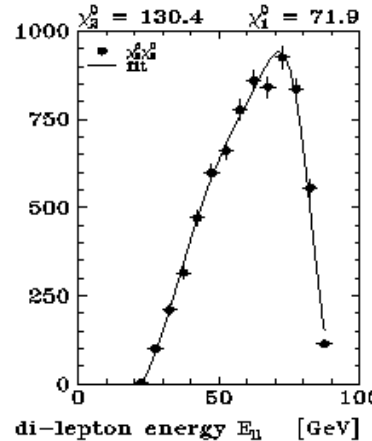
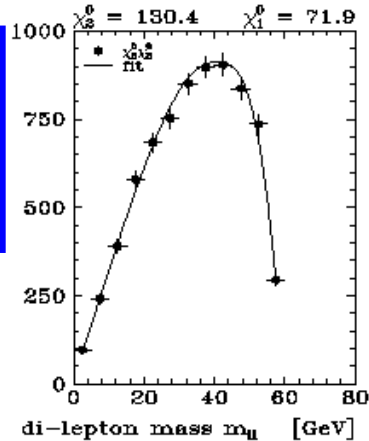
$$e_L^- e_R^+ \rightarrow \tilde{\mu}_L \tilde{\mu}_R \rightarrow \mu \tilde{\chi}_2^0$$



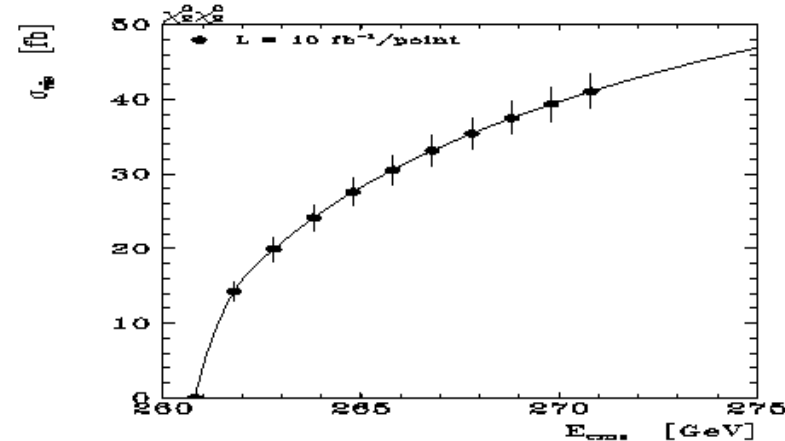
$$E_{\max/\min} = \frac{M_{\tilde{\mu}}}{2} \left( 1 - \frac{M_{\tilde{\chi}_1^0}^2}{M_{\tilde{\mu}}^2} \right) \times \left( 1 \pm \sqrt{1 - \frac{M_{\tilde{\mu}}^2}{E_{\text{beam}}^2}} \right)$$

$$e_L^- e_R^+ \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_2^0 \rightarrow \mu \mu \tilde{\chi}_1^0$$

Precision on  
masses of  
order 0.5-0.1%



$\tilde{\chi}_2^0$  Threshold Scan



# SUSY Sparticle Mass Precision at a LC

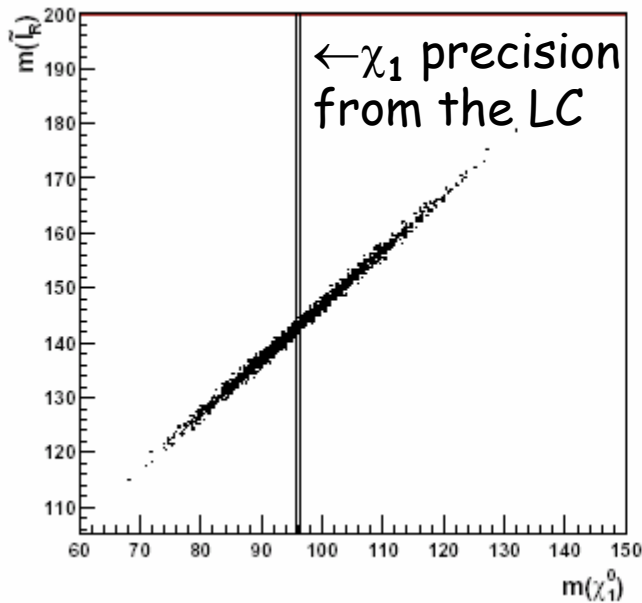
	$m$ [GeV]	$\Delta m$ [GeV]	Comments
$\tilde{\chi}_1^\pm$	176.4	0.55	simulation threshold scan, $100 \text{ fb}^{-1}$
$\tilde{\chi}_2^\pm$	378.2	3	estimate $\tilde{\chi}_1^\pm \tilde{\chi}_2^\mp$ , spectra $\tilde{\chi}_2^\pm \rightarrow Z \tilde{\chi}_1^\pm, W \tilde{\chi}_1^0$
$\tilde{\chi}_1^0$	96.1	0.05	combination of all methods
$\tilde{\chi}_2^0$	176.8	1.2	simulation threshold scan $\tilde{\chi}_2^0 \tilde{\chi}_2^0$ , $100 \text{ fb}^{-1}$
$\tilde{\chi}_3^0$	358.8	3 – 5	spectra $\tilde{\chi}_3^0 \rightarrow Z \tilde{\chi}_{1,2}^0, \tilde{\chi}_2^0 \tilde{\chi}_3^0, \tilde{\chi}_3^0 \tilde{\chi}_4^0$ , $750 \text{ GeV}, > 1000 \text{ fb}^{-1}$
$\tilde{\chi}_4^0$	377.8	3 – 5	spectra $\tilde{\chi}_4^0 \rightarrow W \tilde{\chi}_1^\pm, \tilde{\chi}_2^0 \tilde{\chi}_4^0, \tilde{\chi}_3^0 \tilde{\chi}_4^0$ , $750 \text{ GeV}, > 1000 \text{ fb}^{-1}$
$\tilde{e}_R$	143.0	0.05	$e^- e^-$ threshold scan, $10 \text{ fb}^{-1}$
$\tilde{e}_L$	202.1	0.2	$e^- e^-$ threshold scan $20 \text{ fb}^{-1}$
$\tilde{\nu}_e$	186.0	1.2	simulation energy spectrum, $500 \text{ GeV}, 500 \text{ fb}^{-1}$
$\tilde{\mu}_R$	143.0	0.2	simulation energy spectrum, $400 \text{ GeV}, 200 \text{ fb}^{-1}$
$\tilde{\mu}_L$	202.1	0.5	estimate threshold scan, $100 \text{ fb}^{-1}$ [36]
$\tilde{\tau}_1$	133.2	0.3	simulation energy spectra, $400 \text{ GeV}, 200 \text{ fb}^{-1}$
$\tilde{\tau}_2$	206.1	1.1	estimate threshold scan, $60 \text{ fb}^{-1}$ [36]
$\tilde{t}_1$	379.1	2	estimate $b$ -jet spectrum, $m_{\min}()$ , $1 \text{ TeV}, 1000 \text{ fb}^{-1}$

Table 5.12: Sparticle masses and their expected precisions in Linear Collider experiments, SPS 1a mSUGRA scenario

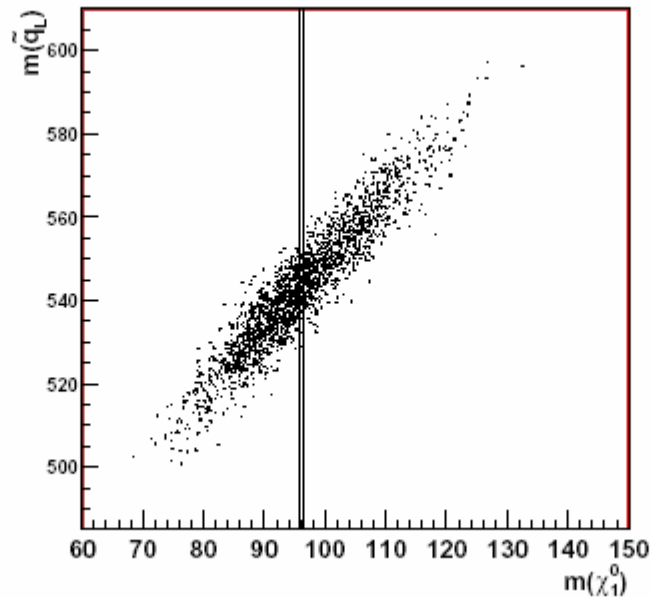
# Mass Determinations including LC data

Improvement of measured particle masses at LHC when the mass of the lightest neutralino is known from the LC

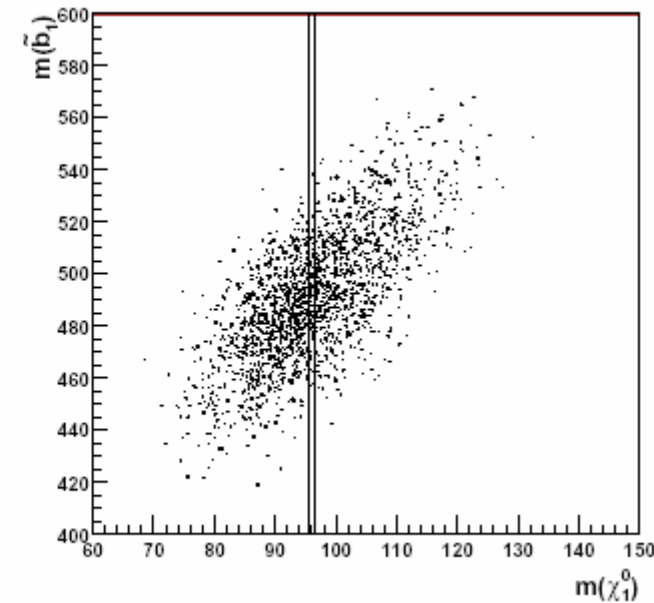
slepton



squark



sbottom



Significant improvements & reduction of correlations

... but correlations between masses will remain

# Combining the LC/LHC Data

300 fb<sup>-1</sup>@LHC

Takes into account 1% energy scale uncertainties

$\Delta M$  values in GeV

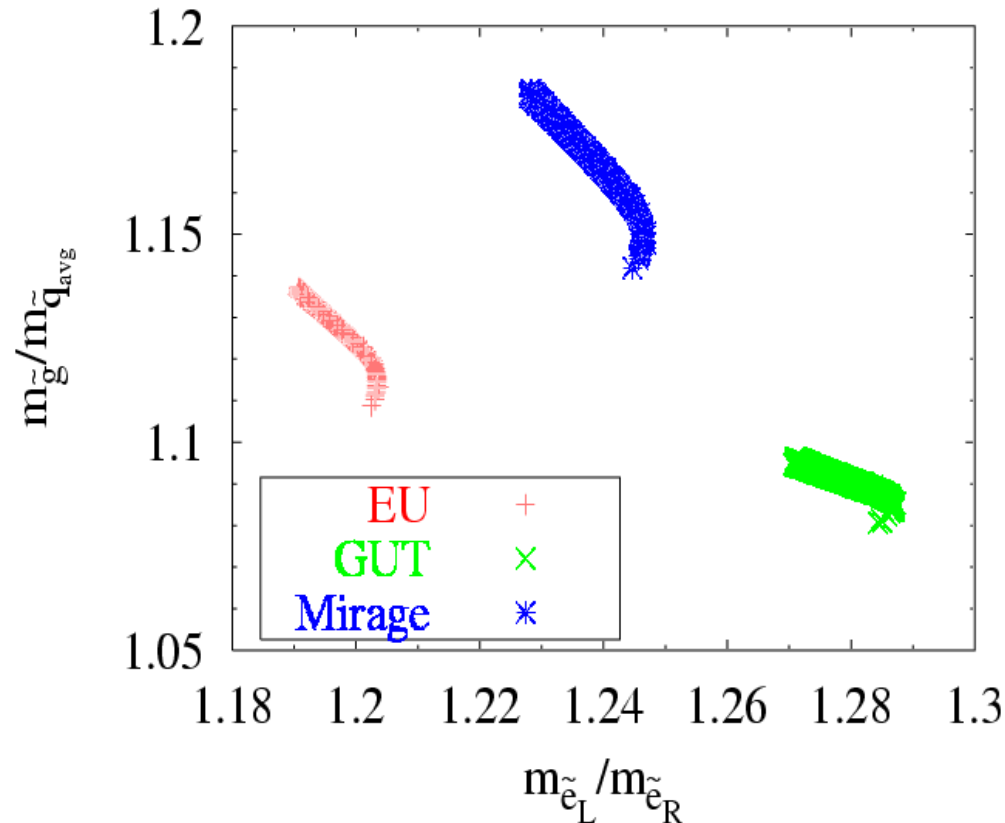
	LHC	LHC+LC
$\Delta m_{\tilde{\chi}_1^0}$	4.8	0.05 (LC input)
$\Delta m_{\tilde{\chi}_2^0}$	4.7	0.08
$\Delta m_{\tilde{\chi}_4^0}$	5.1	2.23
$\Delta m_{\tilde{l}_R}$	4.8	0.05 (LC input)
$\Delta m_{\tilde{\ell}_L}$	5.0	0.2 (LC input)
$\Delta m_{\tilde{\tau}_1}$	5-8	0.3 (LC input)
$\Delta m_{\tilde{q}_L}$	8.7	4.9
$\Delta m_{\tilde{q}_R}$	7-12	5-11
$\Delta m_{\tilde{b}_1}$	7.5	5.7
$\Delta m_{\tilde{b}_2}$	7.9	6.2
$\Delta m_{\tilde{g}}$	8.0	6.5

Significant improvements with an LC/LHC combined data

# Why do we want % precision on masses?

Allanach, Grellscheid, Quevedo

Discrimination between different SUSY-breaking scenarios



Need information of both the squark and slepton sector  
Need % level accuracy to distinguish between different models

# 2. Predict Sparticle Masses from LC → LHC

Kalinowski, Moortgat-pick, Nojiri, Polesello

A step further: predicting sparticle masses from LC data.  
 LC can measure neutral  $\chi_1, \chi_2$  and charged  $\chi_1$  precisely

⇒ Measurements of masses, cross sections and the mixing angles (using polarized beams)

⇒ Determine the SUSY parameters

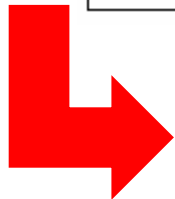
$M_1, M_2$  (U(2) and SU(2) gaugino masses)

$\mu$  (higgsino mixing parameter)

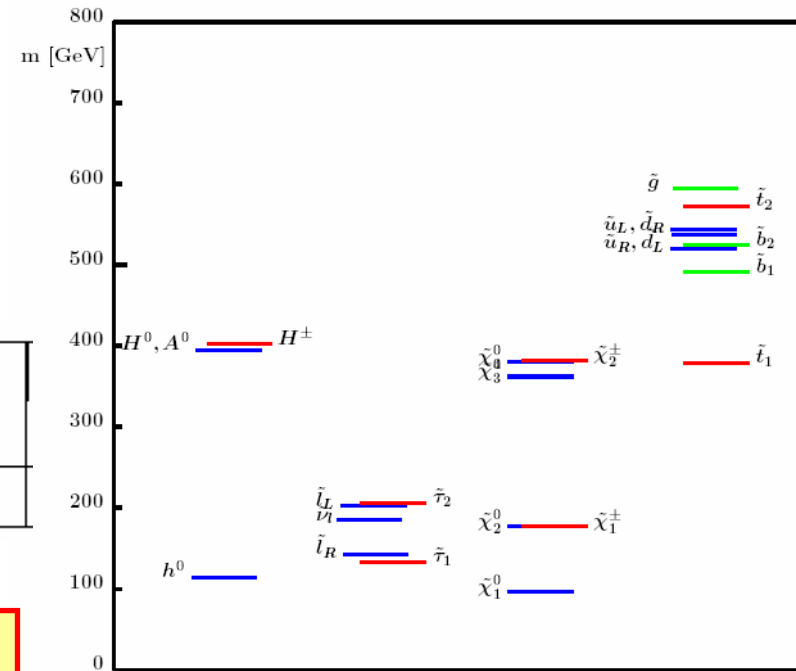
and  $\tan\beta$



SUSY Parameters			
$M_1$	$M_2$	$\mu$	$\tan\beta$
$99.1 \pm 0.2$	$192.7 \pm 0.5$	$352.4 \pm 4.5$	$10.2 \pm 0.9$



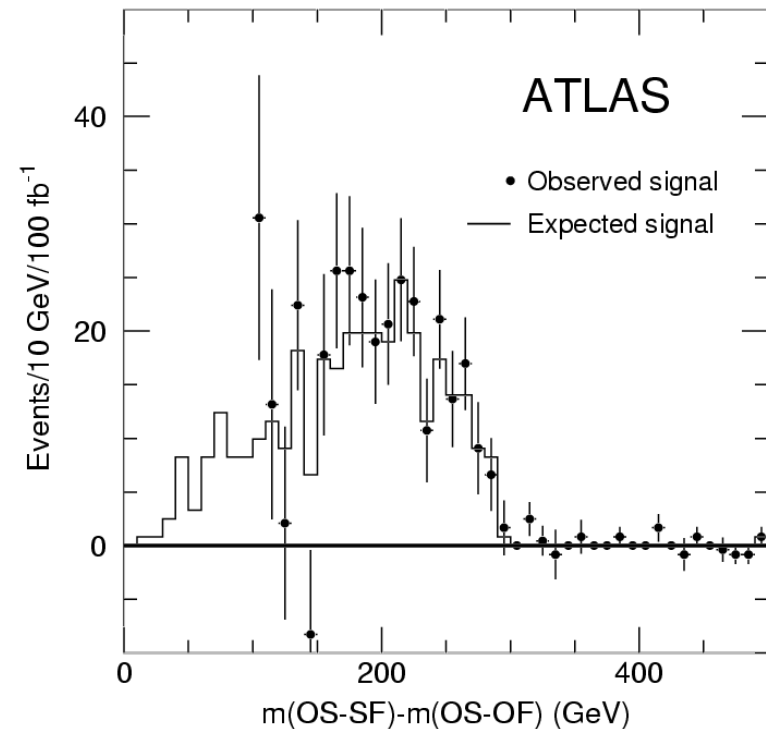
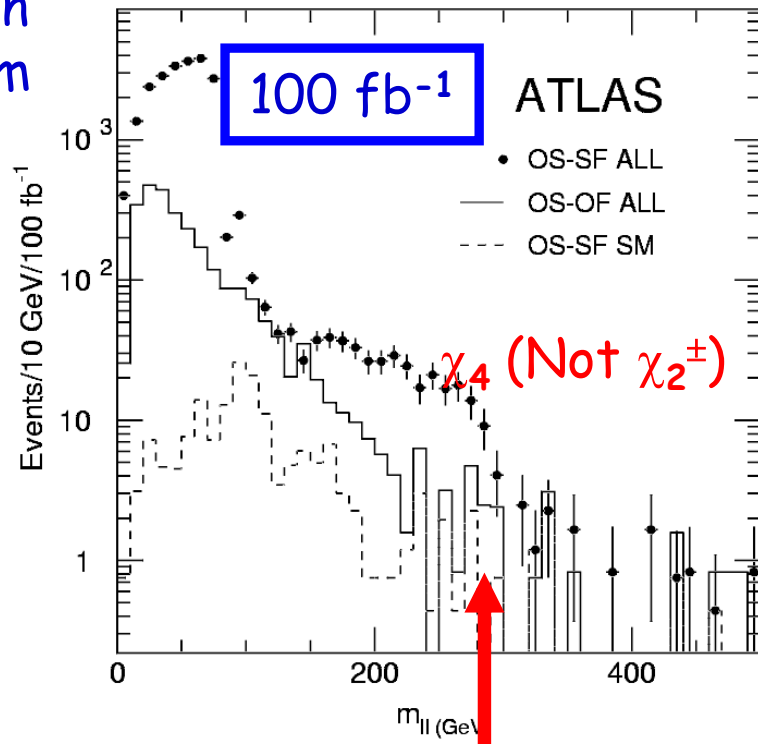
Predicts:  $m(\chi_4) = 378.3 \pm 8.8 \text{ GeV}$



# Finding $\chi_4$ in the LHC Data...

- ⇒ This helps to interpret the LHC data
- ⇒ Marginal edge for  $\chi_4$  at the LHC found with LC input!

Di-lepton spectrum

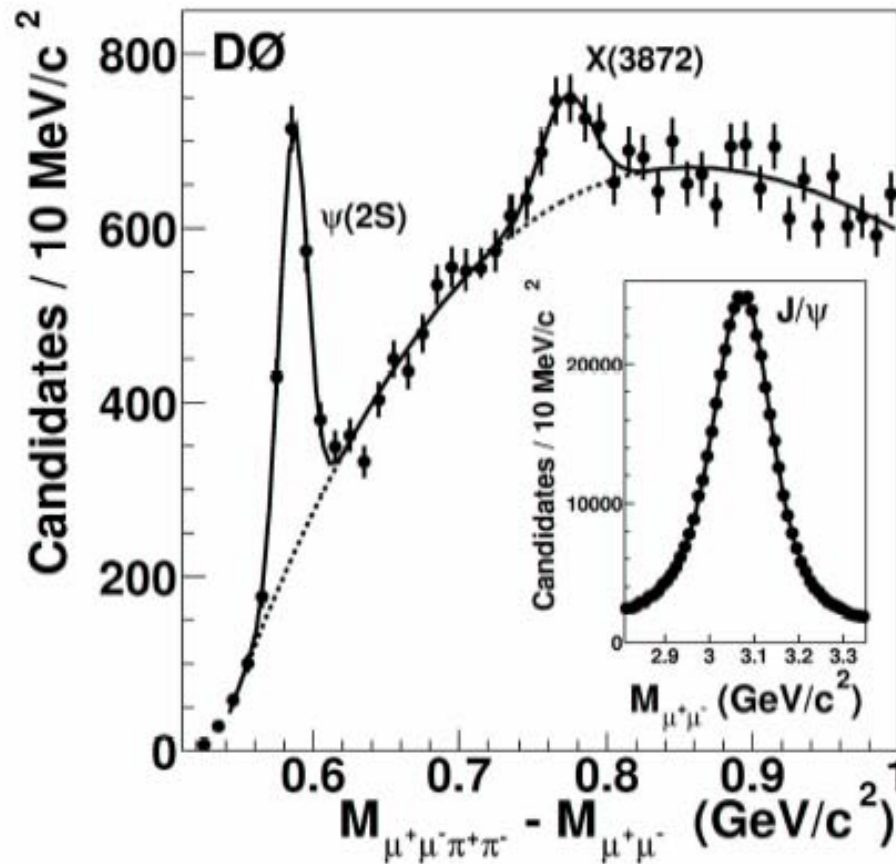


With a tailored analysis can measure  $\Rightarrow m(\chi_4)$  to  $\sim 5$  GeV  
 When  $m(\chi_1)$  is known from the LC then  $\Rightarrow m(\chi_4)$  to 2.2 GeV

Requires machines to run at the same time

# Not a precedent...

2003: Belle ( $e^+e^-$ ) finds X(3872)  $\rightarrow$  D0 and CDF search and find it

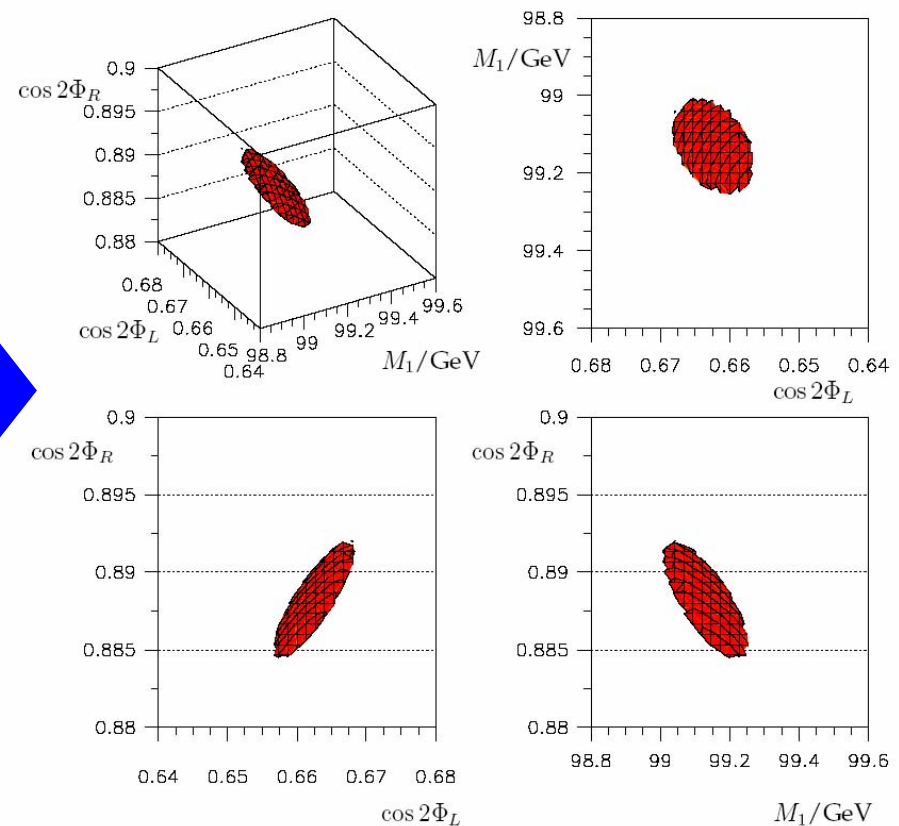
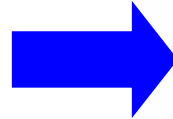
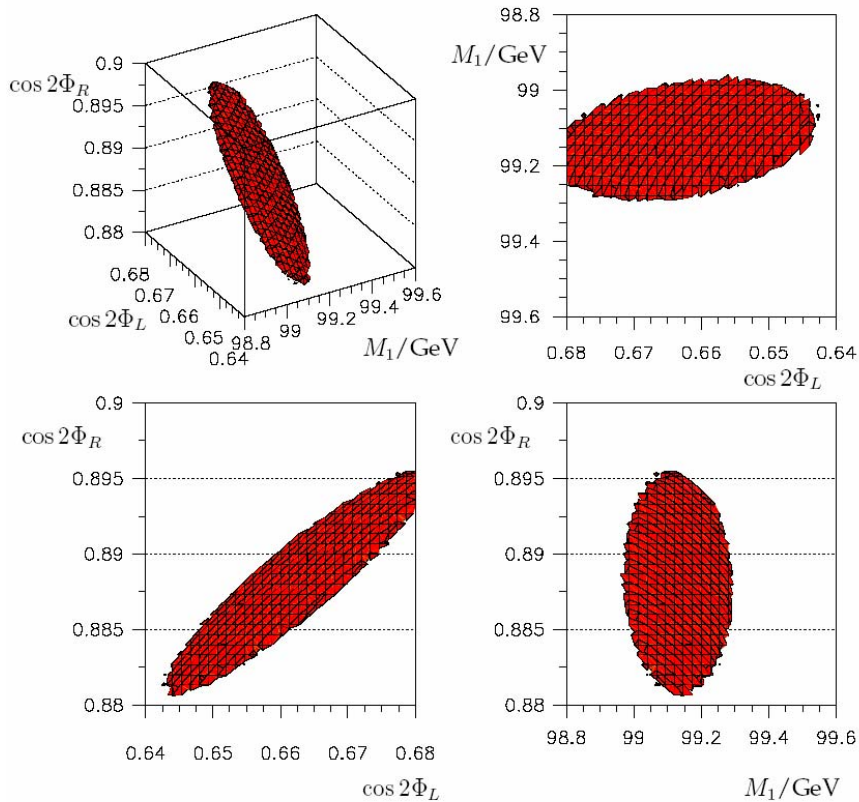


# ...and now.. $\Rightarrow$ use $\chi_4$ for LC data!

LC information alone

$\Delta\chi^2=6$  curves

LHC+LC information



SUSY Parameters			
$M_1$	$M_2$	$\mu$	$\tan\beta$
$99.1 \pm 0.1$	$192.7 \pm 0.3$	$352.4 \pm 2.1$	$10.2 \pm 0.6$

Significant improvement of the precision

# Some Comments

- LC prediction for  $M(\chi_4)$  increases the statistical significance of the LHC: testing only one mass hypothesis rather than many hypotheses.
- A mismatch between LC prediction and LHC measurement can imply (N)MSSM or something entirely different. So it will be important anyway
- **Prototype example of LHC/LC synergy:**
  - A signal with small statistical significance seen at the LHC after LC predicts it, calls for higher luminosity, improved analyses, cuts, perhaps trigger upgrades etc.
  - In such case overlap in LHC/LC running will be very important

# 3. Full Reconstruction of the stop/bottom Parameters with LHC $\otimes$ LC

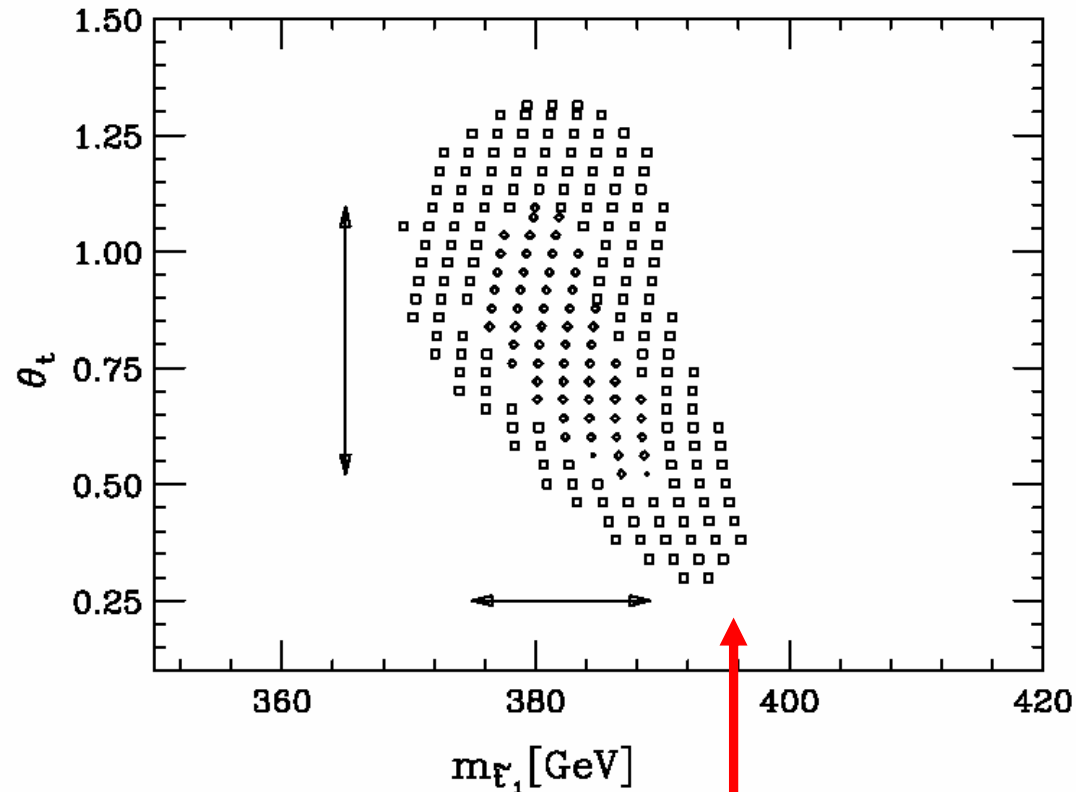
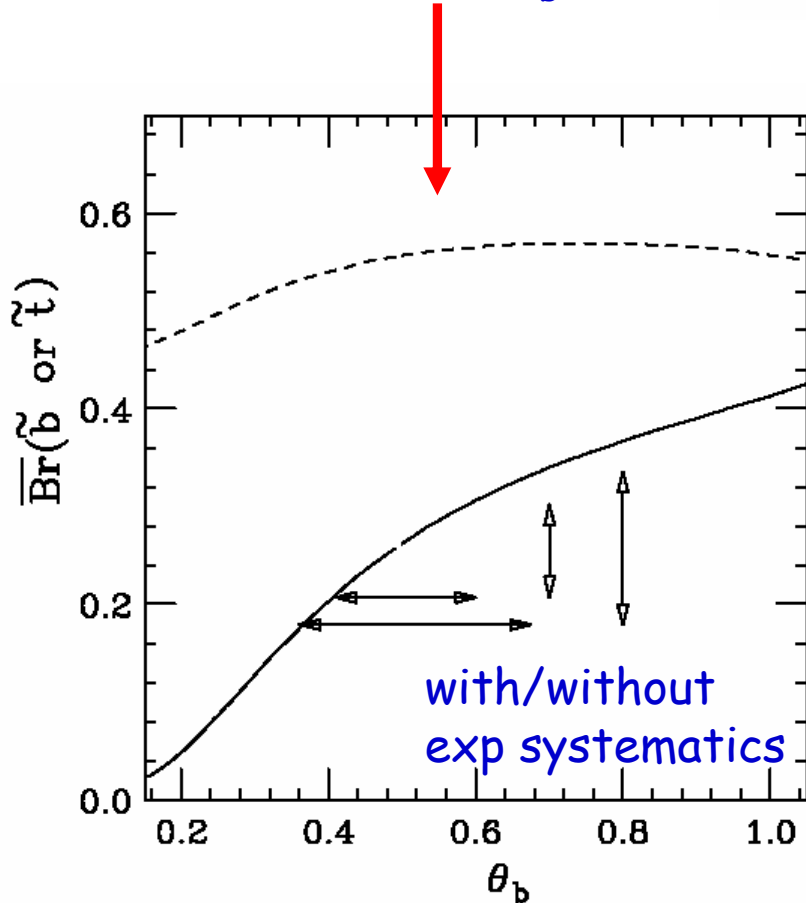
Hisano, Kawagoe, Nojiri

- **Take** the set of electroweak SUSY parameters determined by the LC and LHC data.
- **Take** branching ratios of bottom (stop) measured by the LHC
- **Take**  $m_{b_1}$  and  $m_{b_2}$  from edge study (+ neutralino from the LC)
- **Measure**
  - tb invariant mass distribution
  - rate of "edge events" in  $m_{tb}$  distribution (chargino chain)
  - rate of events in the 2 lepton+b distribution (neutralino-2 chain)

⇒ extract sbottom and stop mixing parameters

# Stop/Sbottom mixing angles

Determination of  $\theta_b$  from  $\text{BR}(\tilde{g} \rightarrow b\tilde{b}_2 \rightarrow bb\tilde{\chi}_2^0) / \text{BR}(\tilde{g} \rightarrow b\tilde{b}_1 \rightarrow bb\tilde{\chi}_2^0)$



Determination of  $\theta_{\text{stop}}, m_{\text{stop}}$  when  $\theta_b$  is known

# 4. Determine the Pattern of SUSY Breaking

	Mass, ideal	"LHC"	"LC"	"LHC+LC"
$\tilde{\chi}_1^\pm$	179.7		0.55	0.55
$\tilde{\chi}_2^\pm$	382.3	-	3.0	3.0
$\tilde{\chi}_1^0$	97.2	4.8	0.05	0.05
$\tilde{\chi}_2^0$	180.7	4.7	1.2	0.08
$\tilde{\chi}_3^0$	364.7		3-5	3-5
$\tilde{\chi}_4^0$	381.9	5.1	3-5	2.23
$\tilde{e}_R$	143.9	4.8	0.05	0.05
$\tilde{e}_L$	207.1	5.0	0.2	0.2
$\tilde{\nu}_e$	191.3	-	1.2	1.2
$\tilde{\mu}_R$	143.9	4.8	0.2	0.2
$\tilde{\mu}_L$	207.1	5.0	0.5	0.5
$\tilde{\nu}_\mu$	191.3	-		
$\tilde{\tau}_1$	134.8	5-8	0.3	0.3
$\tilde{\tau}_2$	210.7	-	1.1	1.1
$\tilde{\nu}_\tau$	190.4	-	-	-
$\tilde{q}_R$	547.6	7-12	-	5-11
$\tilde{q}_L$	570.6	8.7	-	4.9
$\tilde{t}_1$	399.5		2.0	2.0
$\tilde{t}_2$	586.3		-	
$\tilde{b}_1$	515.1	7.5	-	5.7
$\tilde{b}_2$	547.1	7.9	-	6.2
$\tilde{g}$	604.0	8.0	-	6.5
$h^0$	110.8	0.25	0.05	0.05
$H^0$	399.8		1.5	1.5
$A^0$	399.4		1.5	1.5
$H^\pm$	407.7	-	1.5	1.5

With all LC/LHC information  $\Rightarrow$   
Determine the SUSY Parameters

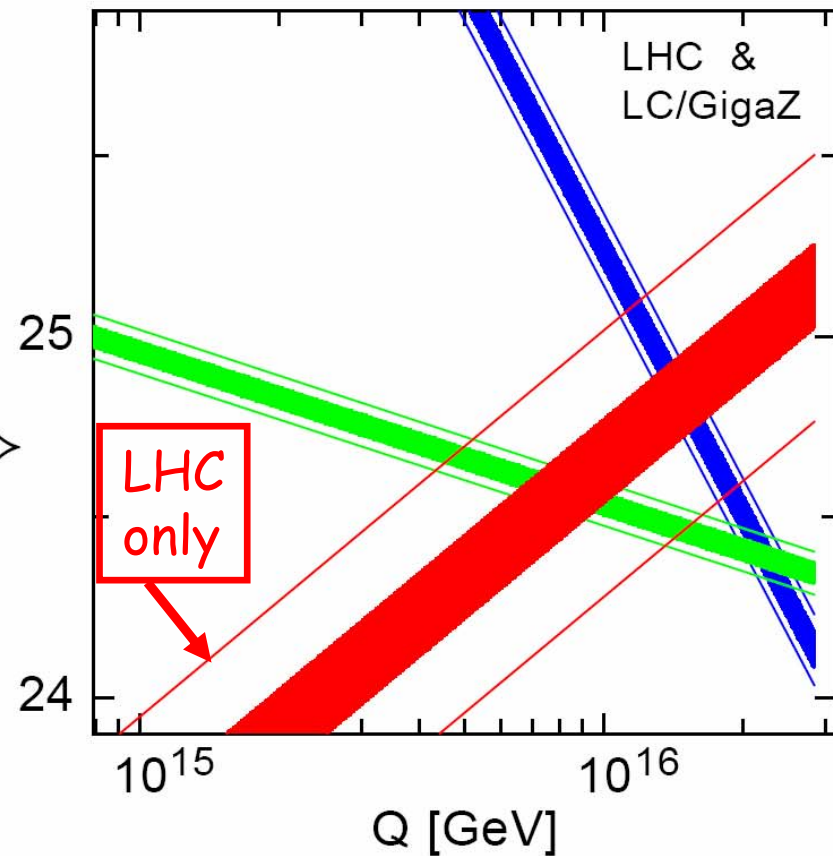
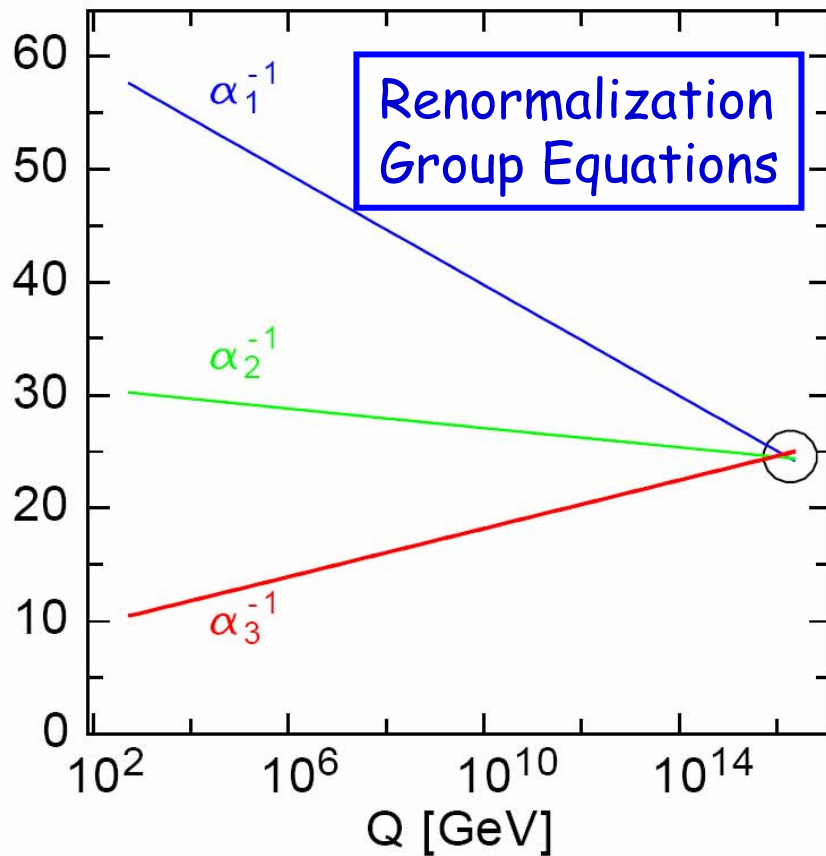


Low energy  
SUSY  
parameters

	Parameter, ideal	"LHC+LC" errors
$M_1$	101.66	0.08
$M_2$	191.76	0.25
$M_3$	584.9	3.9
$\mu$	357.4	1.3
$M_{L_1}^2$	$3.8191 \cdot 10^4$	82.
$M_{E_1}^2$	$1.8441 \cdot 10^4$	15.
$M_{Q_1}^2$	$29.67 \cdot 10^4$	$0.32 \cdot 10^4$
$M_{U_1}^2$	$27.67 \cdot 10^4$	$0.86 \cdot 10^4$
$M_{D_1}^2$	$27.45 \cdot 10^4$	$0.80 \cdot 10^4$
$M_{L_3}^2$	$3.7870 \cdot 10^4$	360.
$M_{E_3}^2$	$1.7788 \cdot 10^4$	95.
$M_{Q_3}^2$	$24.60 \cdot 10^4$	$0.16 \cdot 10^4$
$M_{U_3}^2$	$17.61 \cdot 10^4$	$0.12 \cdot 10^4$
$M_{D_3}^2$	$27.11 \cdot 10^4$	$0.66 \cdot 10^4$
$M_{H_1}^2$	$3.25 \cdot 10^4$	$0.12 \cdot 10^4$
$M_{H_2}^2$	$-12.78 \cdot 10^4$	$0.11 \cdot 10^4$
$A_t$	-497.	9.
$\tan \beta$	10.0	0.4

# Check the Unification of the Couplings

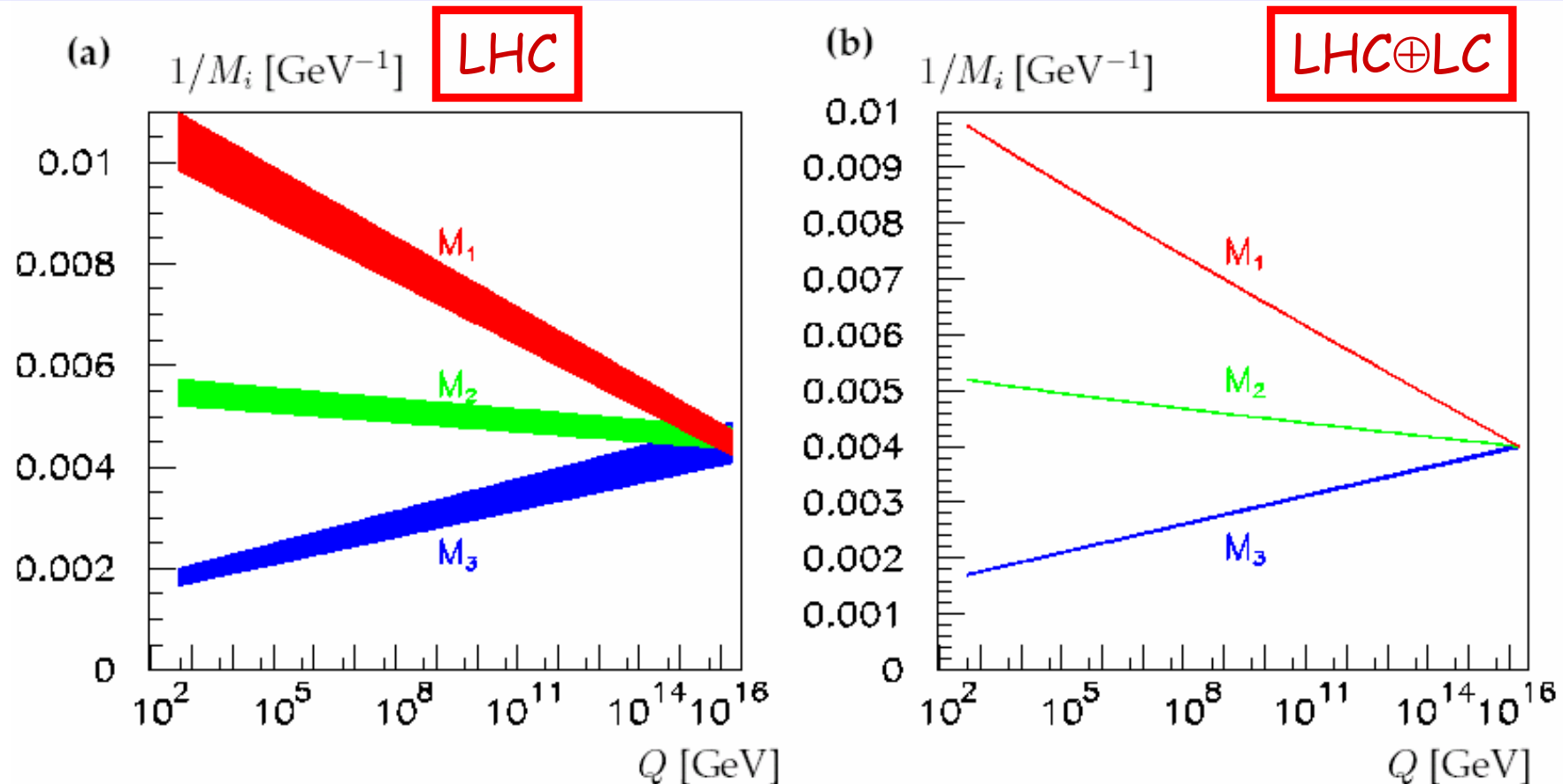
Input SUSY spectrum parameters and + present data on  $\alpha, \alpha_s, \sin^2\theta\dots$



# Extrapolation to Physics at High Scales

Blair, Martyn, Polesello, Porod, Zerwas

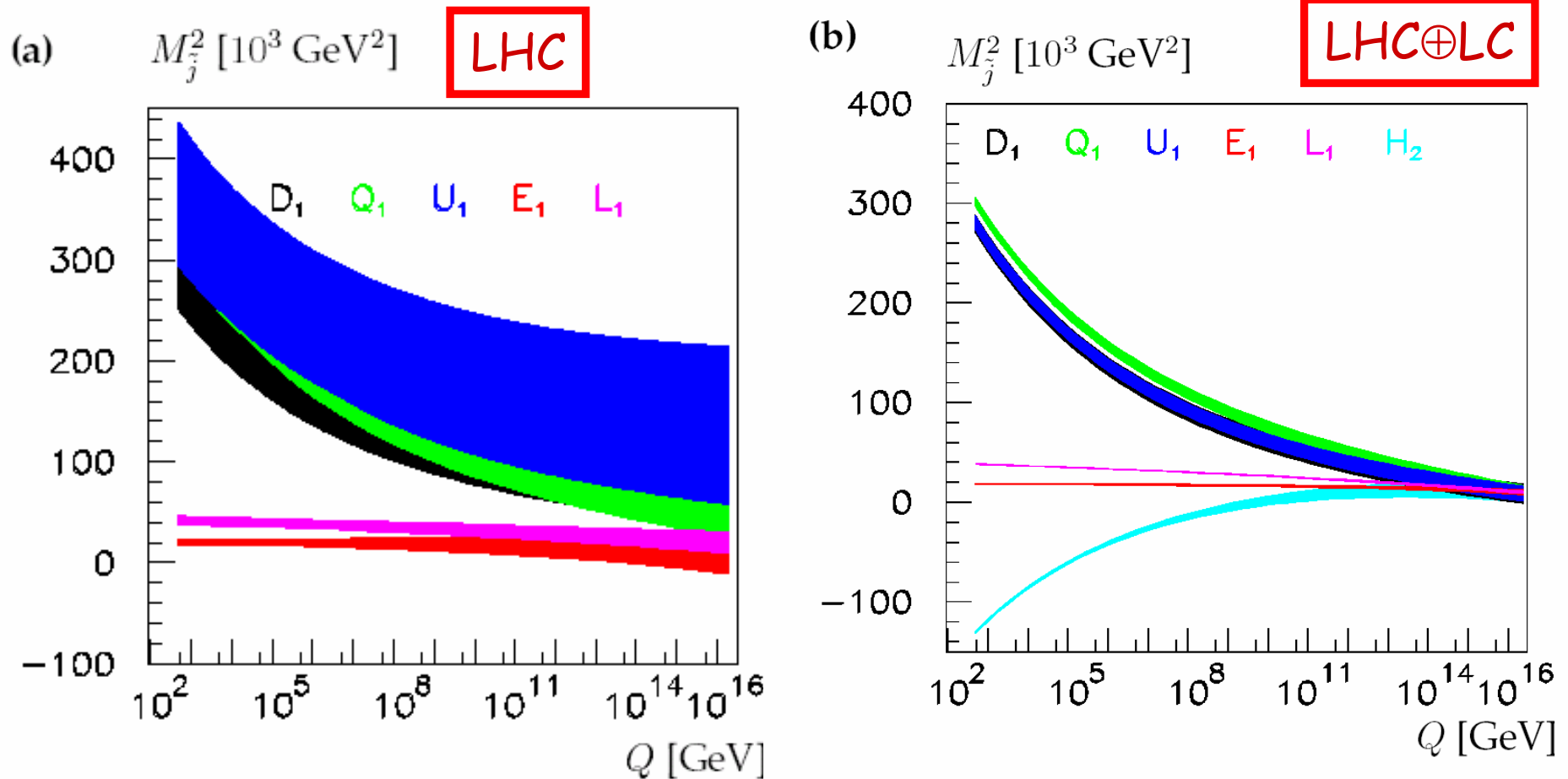
From a combination of LHC and LC results, precise measurements of masses of SUSY particles, couplings: Evolution of gaugino mass parameters



Model independent bottom-up approach: combined information on low-energy SUSY parameters as input to the Renormalization Group Equation evolution

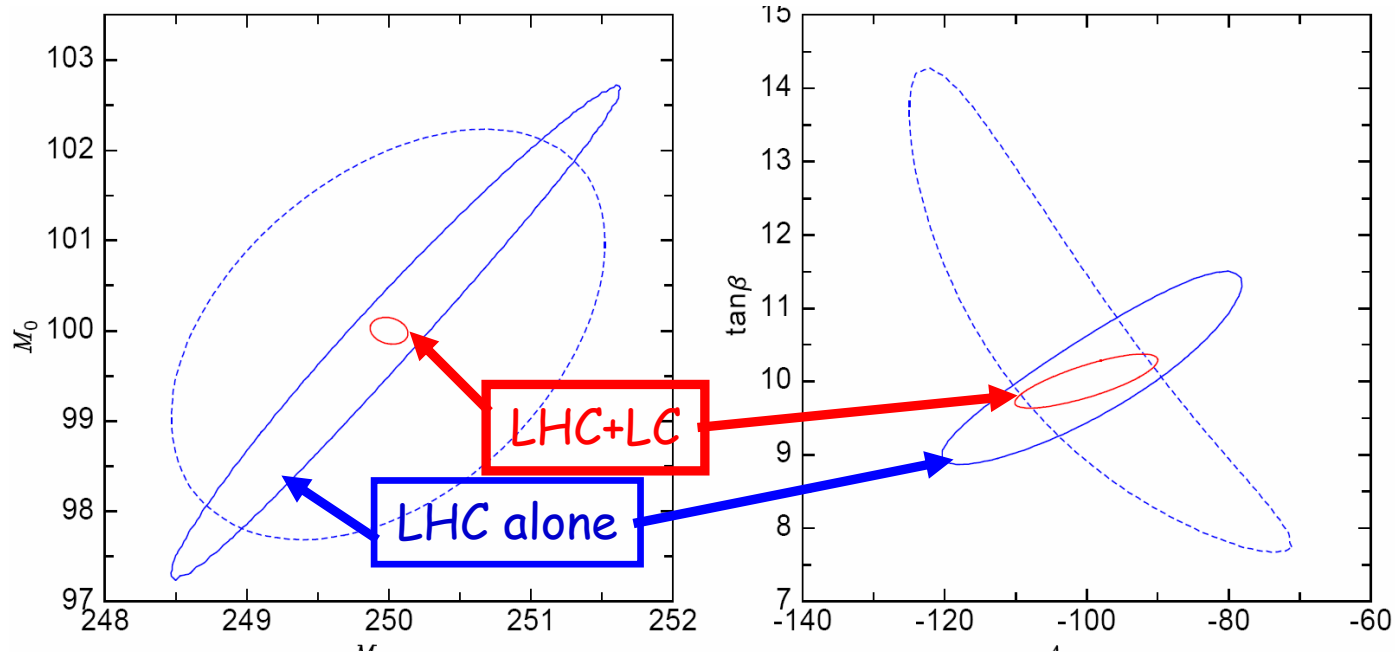
# Extrapolation to Physics at High Scales

From a combination of LHC and LC results, precise measurements of masses of SUSY particles, couplings: **Evolution of sfermion mass parameters**



# Precision on MSUGRA Parameters

$M_0, M_{1/2}, \tan\beta, A_0, \text{sign}(\mu)$  are the MSUGRA parameters

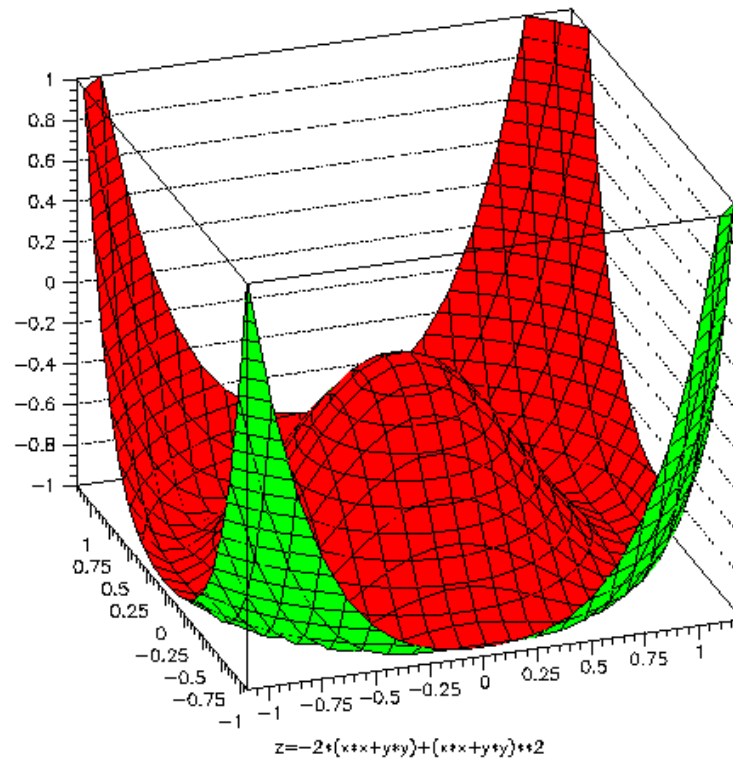


	"LHC"	"LC"	"LHC+LC"
$M_{1/2}$	$250.0 \pm 2.1$	$250.0 \pm 0.4$	$250.0 \pm 0.2$
$M_0$	$100.0 \pm 2.8$	$100.0 \pm 0.2$	$100.0 \pm 0.2$
$A_0$	$-100.0 \pm 34$	$-100.0 \pm 27$	$-100.0 \pm 14$
$\tan\beta$	$10.0 \pm 1.8$	$10.0 \pm 0.6$	$10.0 \pm 0.4$

## Few Remarks on these SUSY Studies

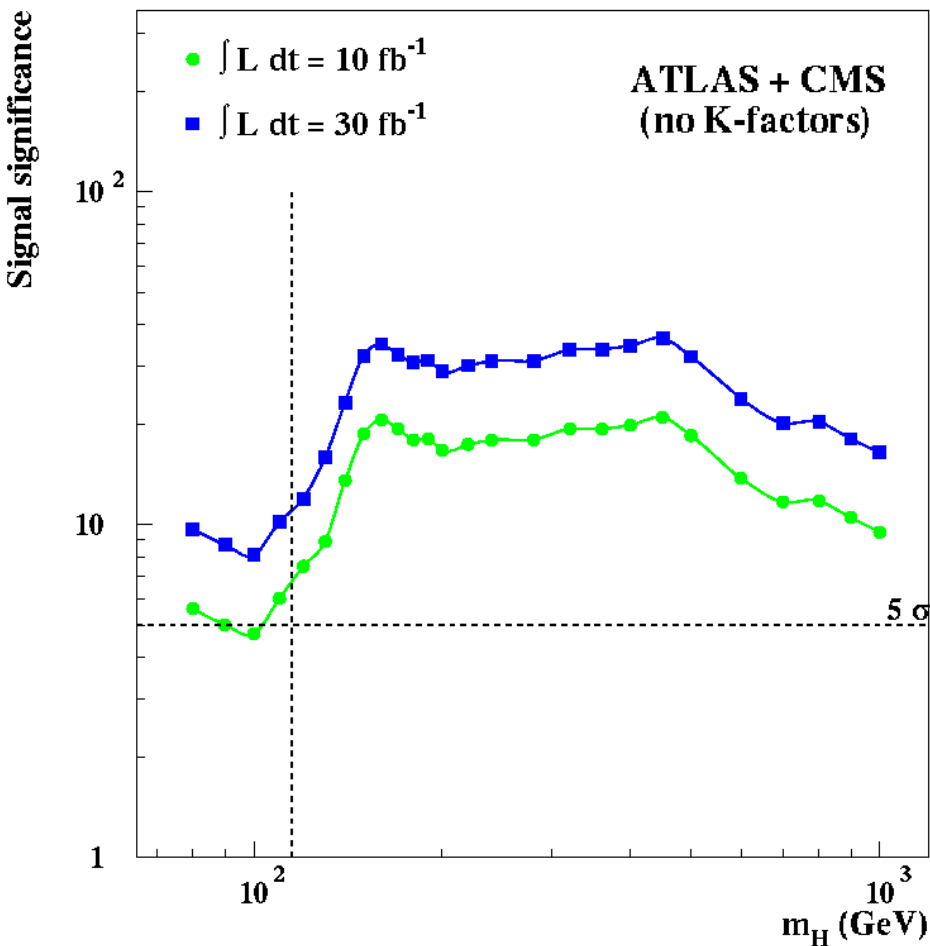
- All studies done (coherently) for SPS1a!
- In future we need to study also less favorable points.
  - ⇒ The impact of a LC/LHC synergy may be even larger for “less favorable” SUSY points, e.g. points at large  $\tan \beta$ 
    - lots of decays into  $\tau$  leptons
    - more difficult at the LHC

## 2. Higgs Physics



# Higgs Measurement Prospects

Discovery in full range with  $10 \text{ fb}^{-1}$



LHC

- $\Delta M/M = 0.1-1\%$  large region
- $\Delta\Gamma/\Gamma = 5-8\%$  ( $M_H > 2M_Z$ )  
=  $\sim 20\%$  ( $M_H < 2M_Z$ )
- Ratios of couplings: 10-20%

LC

- $\Delta M/M = 0.03\%$
- Total width
- Invisible width ( $ee \rightarrow ZH$ )
- Absolute couplings: few %
- Higgs self coupling 20 %
- ...

# 1. Combine LHC Data on Heavy Higgs with LC Data on the Light Higgs

Desch, Gross, Heinemeyer, Weiglein

SPS1b  $\tan\beta=30$

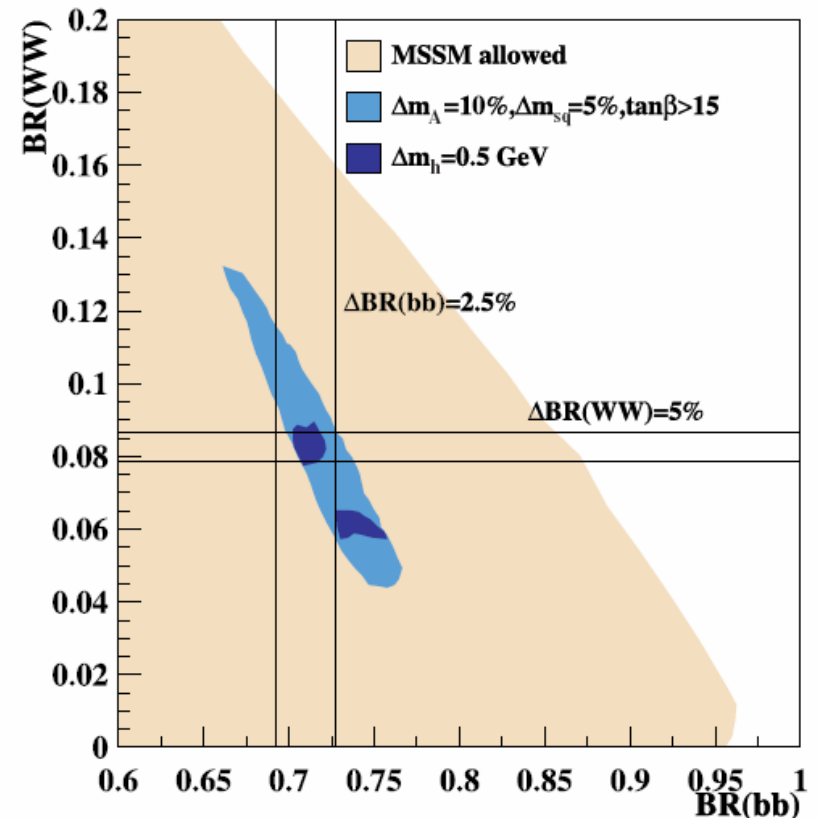
**Assume:**

LHC information on  $M_A$  and  $\tan\beta$

⊕ (LHC⊗LC) information on stop/bottom masses

⊕ LHC/LC measurement of  $m_H$

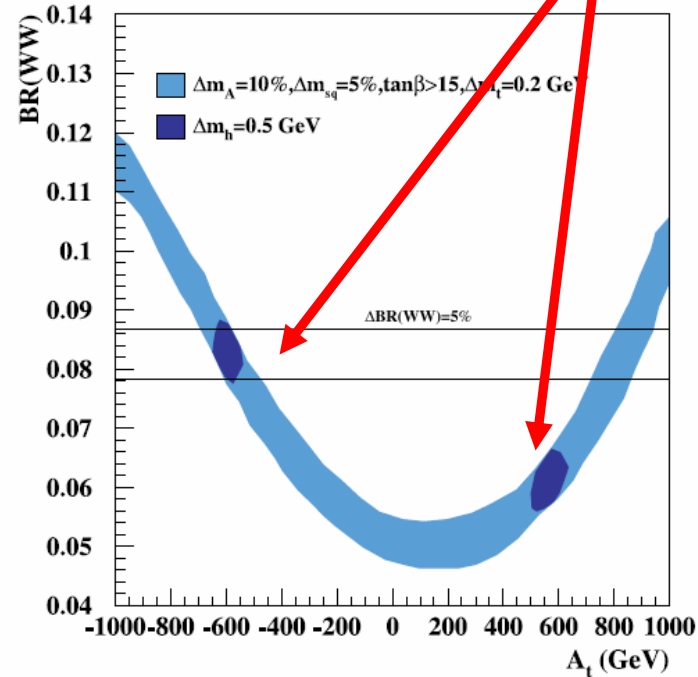
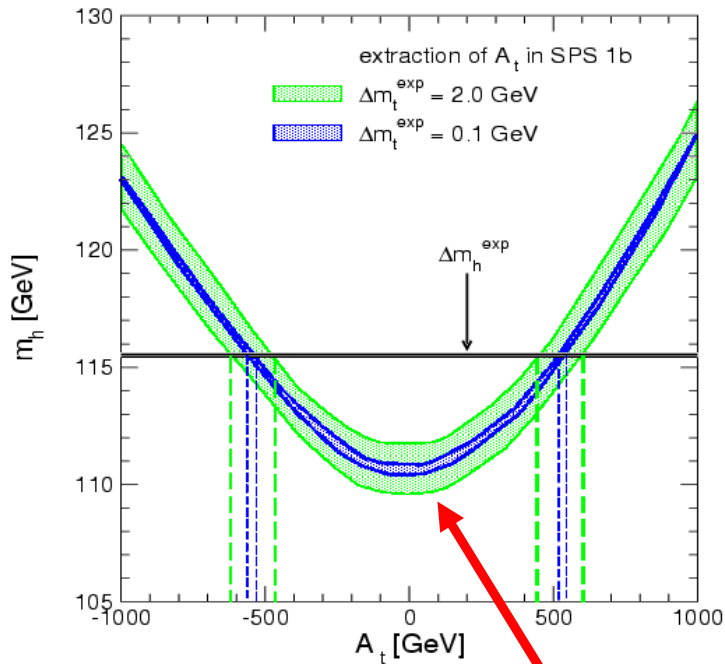
⊕ LC information on  $m_{\text{top}} \sim 0.1 \text{ GeV}$



Comparison of MSSM predictions based on LHC data with BR's measured at the LC leads to very sensitive tests.

# Trilinear Coupling $A_t$

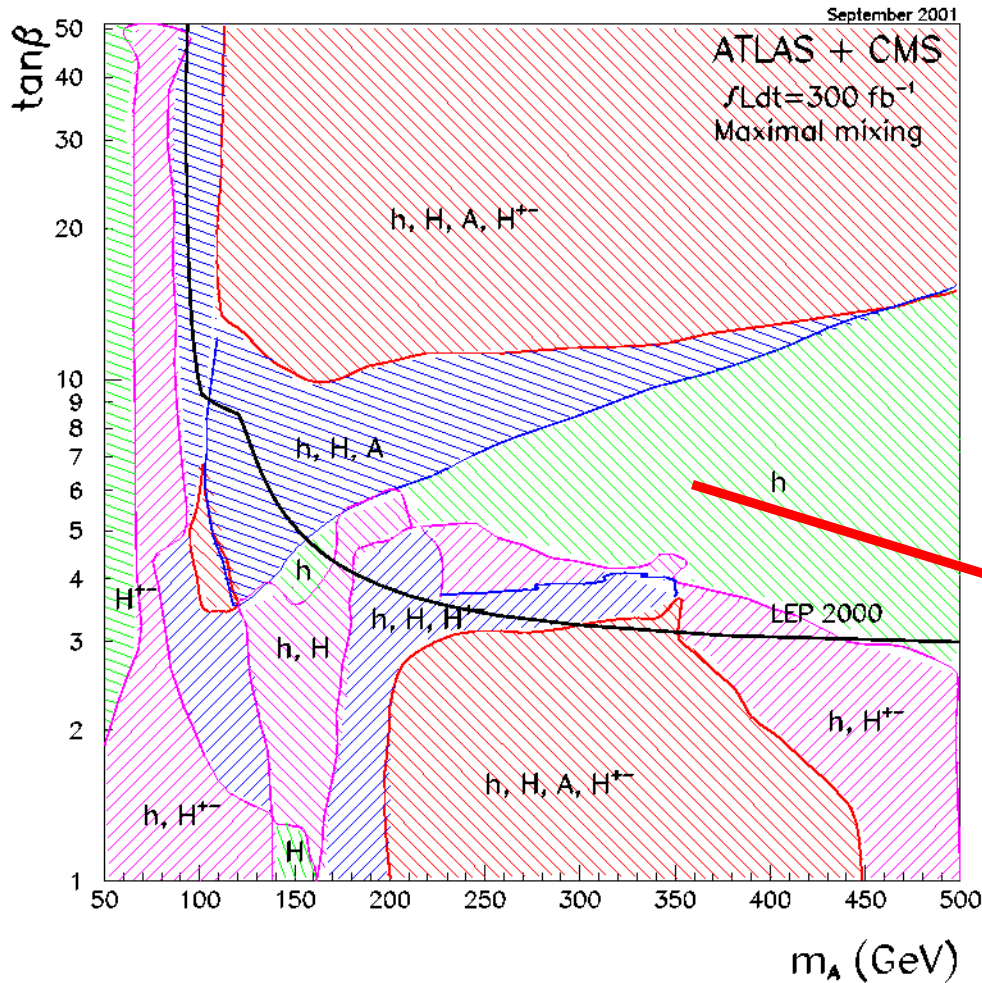
If  $m_{\text{stop}}$  and  $m_{\text{bottom}}$  measured  
 $\Rightarrow m_H$  allows for an indirect determination of  $A_t$  (up to a sign)



Precise measurement of  $m_t$  at the LC crucial:  $\Delta m_t \sim 100 \text{ MeV}$   
 $\Rightarrow \Delta m_t^{\text{LC}} \text{ vs } \Delta m_t^{\text{LHC}} \Rightarrow \text{accuracy of } A_t \text{ determination improved by factor 3}$

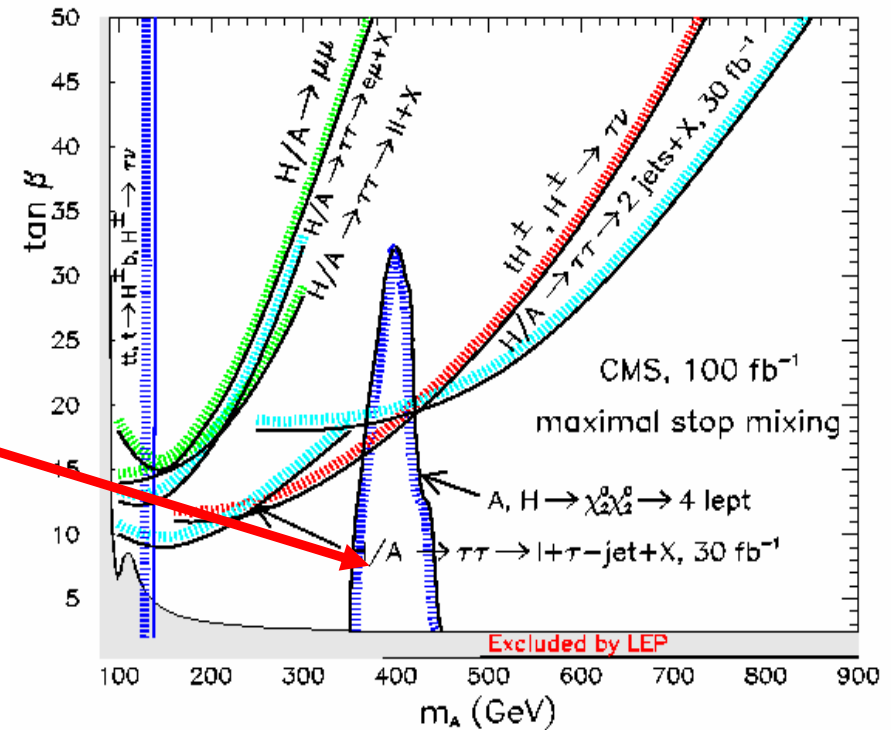
# 2. Heavy MSSM Higgs

Plot for 5  $\sigma$  discovery



At low  $\tan \beta$ , we may exploit the sparticle decay modes:

$$A, H \rightarrow \chi_2^0 \chi_2^0 \rightarrow 4l + E_T^{miss}$$



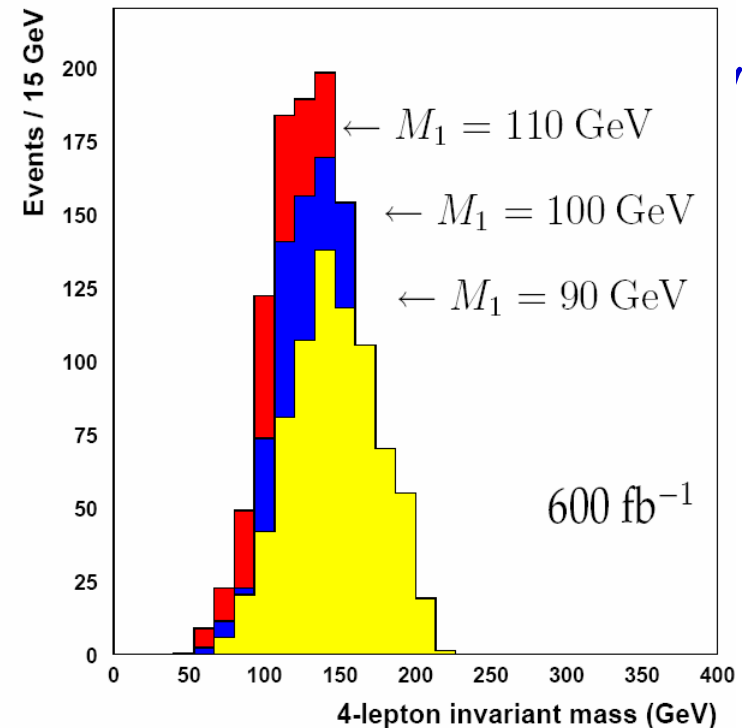
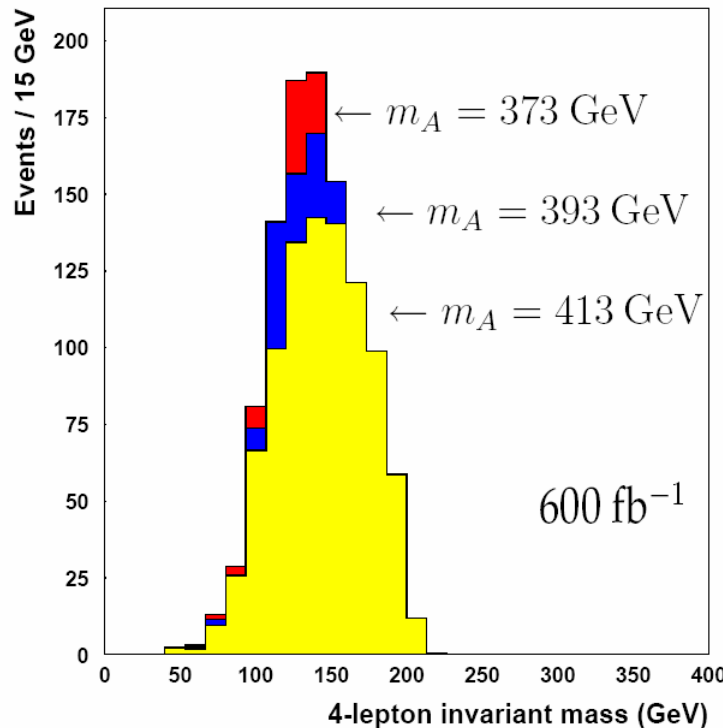
# Reconstruct $M_A$

Moortgat

$$H, A \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_2^0$$

→ 4 leptons and missing  $E_T$

Get mass from sensitivity to the four lepton invariant mass

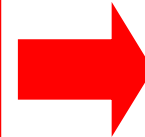


LHC: Sensitivity dominated by uncertainty at the LSP mass knowledge  
LHC⊗LC : Sensitive to  $M_A \sim 3\%$  if mass of LSP known to better than 1%

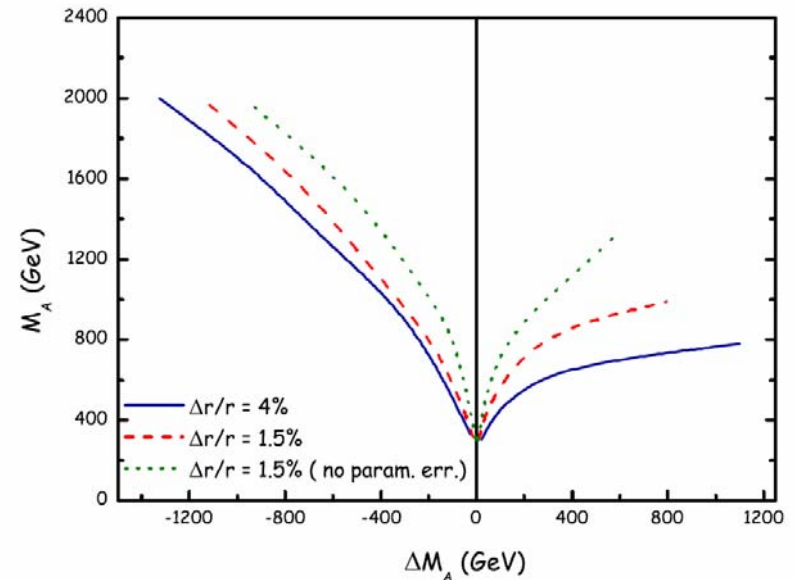
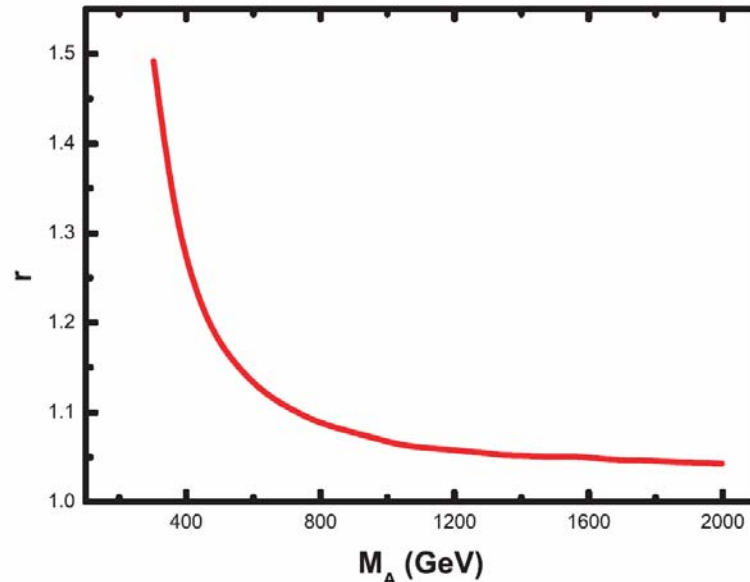
# 3. Constraining $M_A$ from LHC and LC Measurements

- Suppose LHC sees only one Higgs and some SUSY particles, but not the  $A/H$  Higgses (SPS1a, but  $M_A$  as a free parameter)
- Use information from the measured SUSY spectrum at LC & LHC and from measured BR of the Higgs measured at LC to predict mass of  $M_A$  (mass of the gluino, sbottom quarks, light stop, Higgs and  $\tan \beta$ )
- Compare :

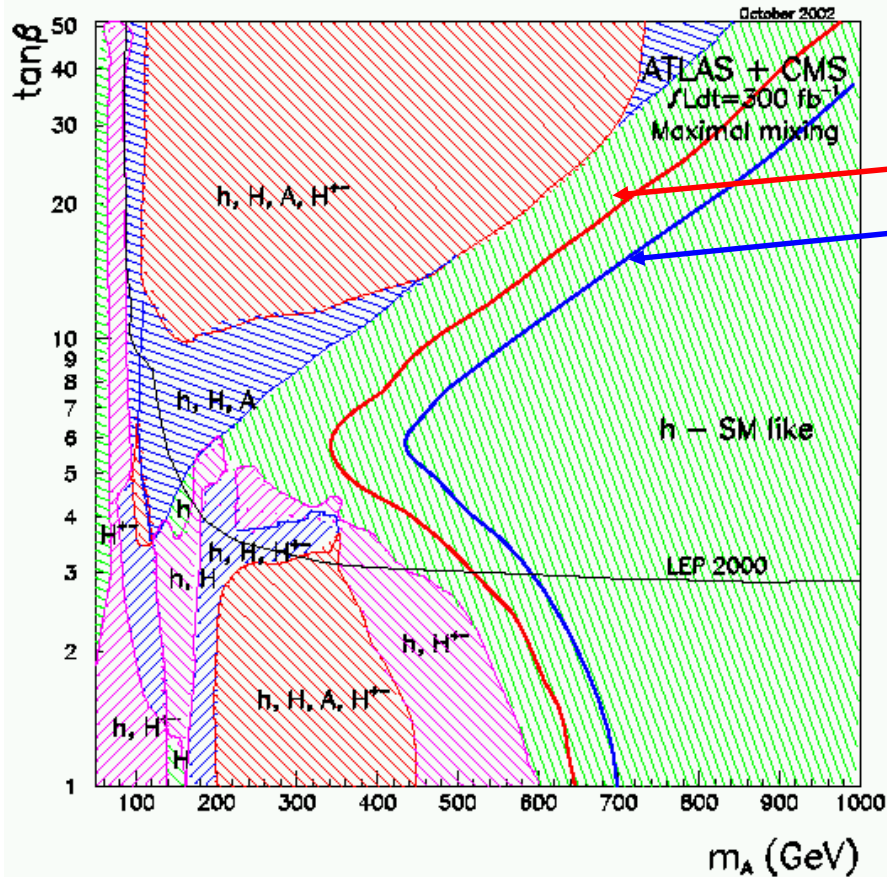
$$r \equiv \frac{\left[ \text{BR}(h \rightarrow b\bar{b}) / \text{BR}(h \rightarrow WW^*) \right]_{\text{MSSM}}}{\left[ \text{BR}(h \rightarrow b\bar{b}) / \text{BR}(h \rightarrow WW^*) \right]_{\text{SM}}}$$



Determine  $M_A$   
with 20-30% for  
 $M_A$  600-800 GeV



# MSSM Higgs search with a LHC upgrade



In the green region only SM-like  $h$  observable with  $300 \text{ fb}^{-1}/\text{exp}$   
Red line: extension with  $3000 \text{ fb}^{-1}/\text{exp}$   
Blue line: 95% excl. with  $3000 \text{ fb}^{-1}/\text{exp}$



Factor 10 increase in luminosity:  
Heavy Higgs observable region  
increases by  $\sim 100 \text{ GeV}$ .



If LC predicts e.g.  $M_A \sim 600 \text{ GeV}$  (for  $\tan\beta = 15$ ) then the  $A$  boson within reach of the LHC with sufficient luminosity

# 4. Top Yukawa Coupling

Dawson, Desch, Juste, Rainwater, Reina, Schumacher, Wackerroth

Assume a light Higgs  $< 2m_t$

Production processes

LC:  $e^+e^- \rightarrow t\bar{t}H$  No precise measurement at 350-500 GeV LC

LHC:  $gg \rightarrow t\bar{t}H$  measures  $\sigma \cdot BR$

studied for  $t\bar{t}b\bar{b}$  and  $t\bar{t}WW$  final states  
depends on  $g_{t\bar{t}H}^2$ ,  $g_{b\bar{b}H}^2$  and  $g_{t\bar{t}H}^2$ ,  $g_{WWH}^2$



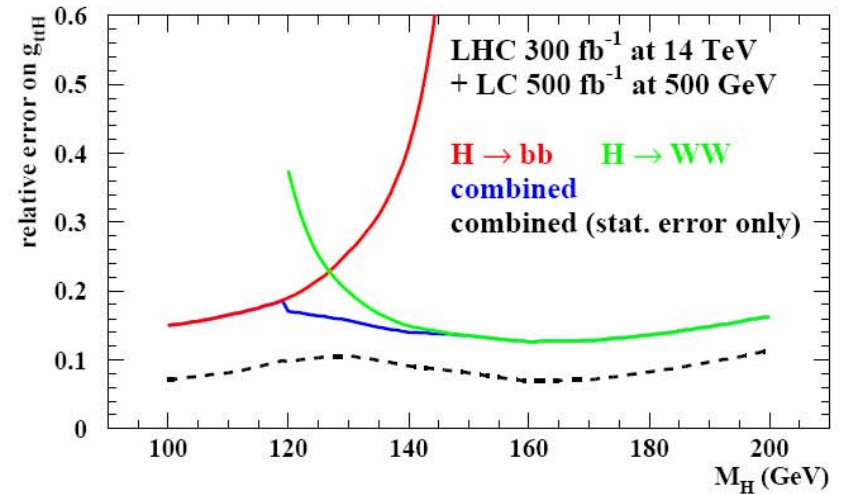
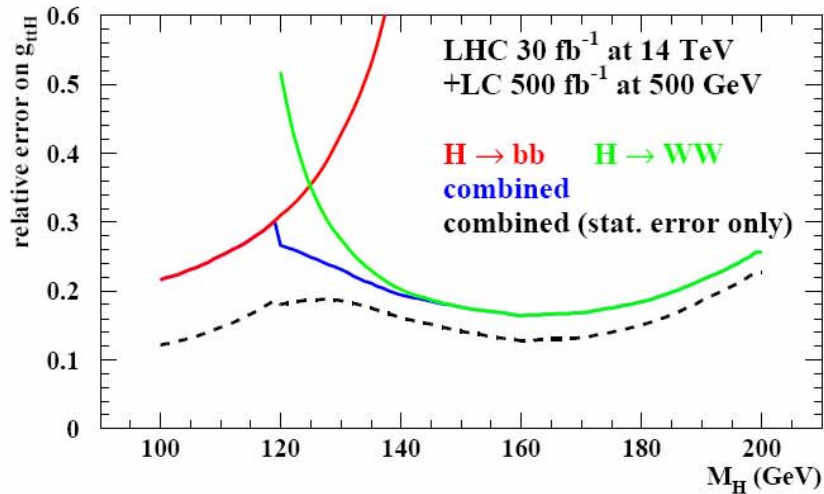
$g_{b\bar{b}H}^2$  and  $g_{WWH}^2$  can be measured precisely in a model independent way at a LC (few %)

$m_H$ (GeV)	$\Delta BR(bb)/BR(bb)$	$\Delta BR(WW)/BR(WW)$
100	0.024	
120	0.024	0.051
140	0.026	0.025
160	0.065	0.021
200		0.021

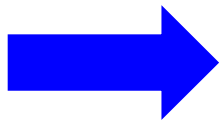
LC  
350 GeV  
500 fb<sup>-1</sup>

⇒ can determine  $g_{t\bar{t}H}^2$  without any model assumptions

# Top Yukawa Coupling



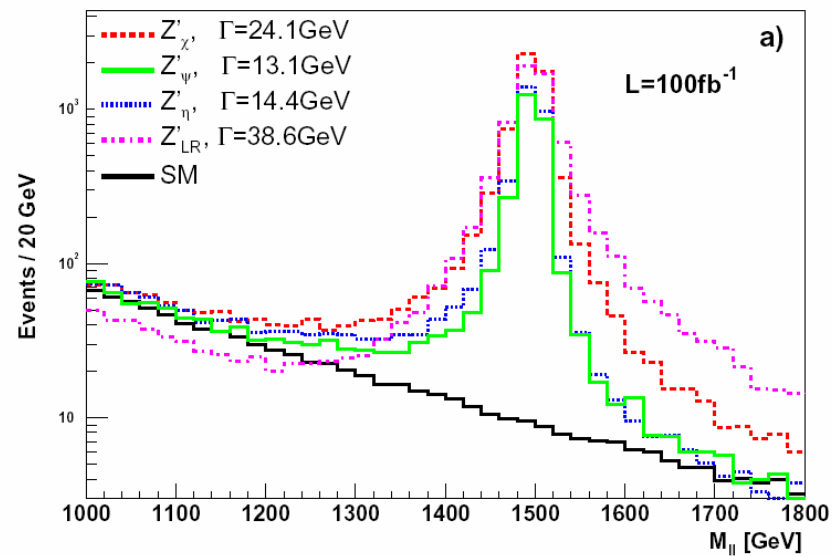
Precision  
of the top  
Yukawa coupling



$m_H$ (GeV)	30 fb <sup>-1</sup>			300 fb <sup>-1</sup>		
	bb	WW	bb+WW	bb	WW	bb + WW
100	0.22(0.12)			0.15(0.07)		
110	0.25(0.15)			0.17(0.08)		
120	0.31(0.19)	0.52(0.49)	0.27(0.18)	0.19(0.10)	0.38(0.31)	0.17(0.10)
130	0.43(0.28)	0.28(0.25)	0.23(0.19)	0.26(0.15)	0.20(0.15)	0.16(0.11)
140	0.72(0.50)	0.20(0.17)	0.19(0.16))	0.41(0.26)	0.15(0.10)	0.14(0.09)
150		0.18(0.14)		1.88(1.21)	0.14(0.08)	0.14(0.08)
160		0.16(0.13)			0.13(0.07)	
170		0.17(0.13)			0.13(0.07)	
180		0.18(0.15)			0.14(0.08)	
190		0.22(0.19)			0.15(0.10)	
200		0.26(0.23)			0.16(0.11)	

~15%

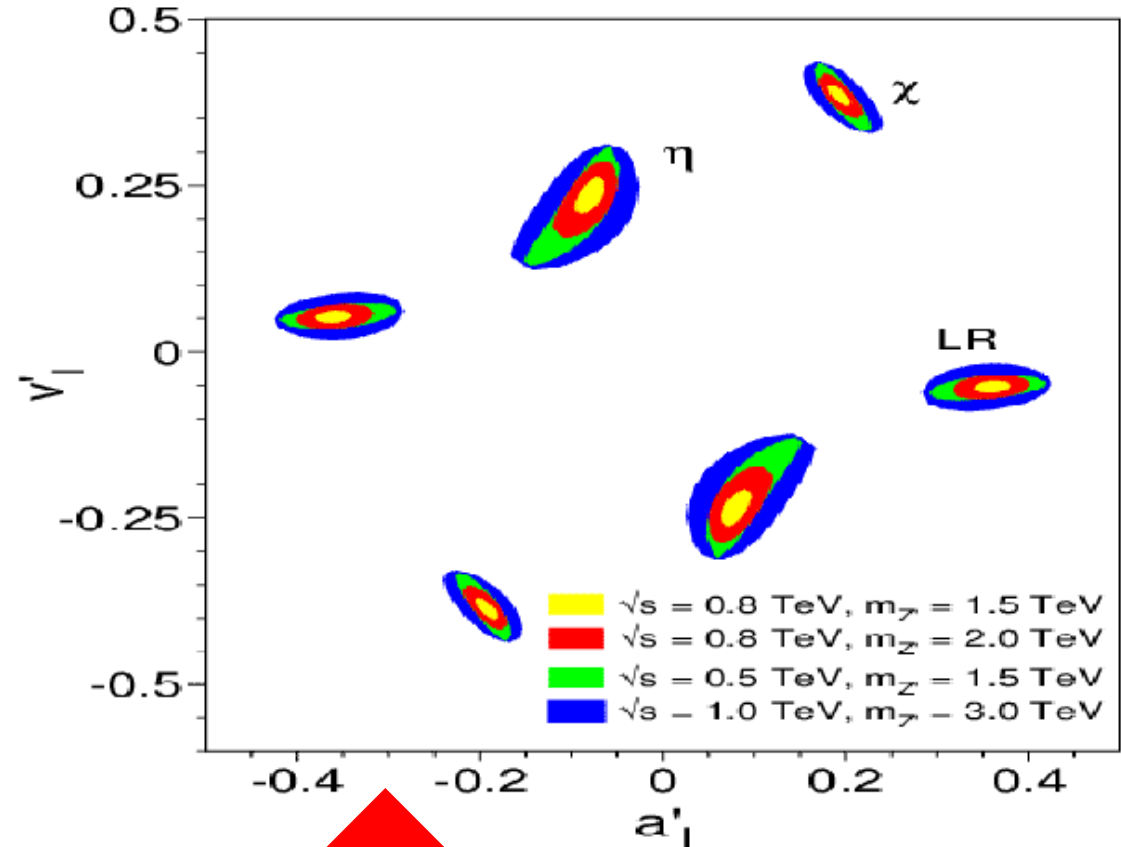
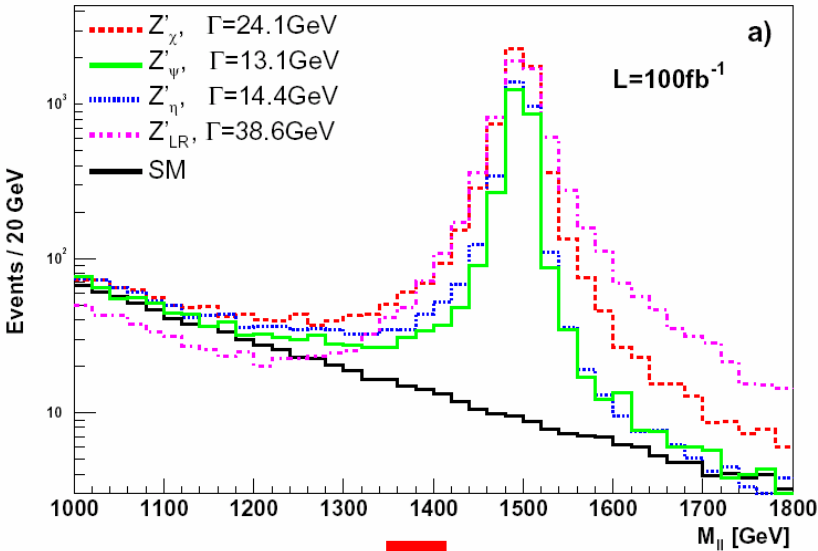
# 3. New Gauge Theories



# New Gauge Theories

Dilepton invariant mass spectrum

Bourlikov, Godfrey, Hewett, Richard, Riemann, Rizzo

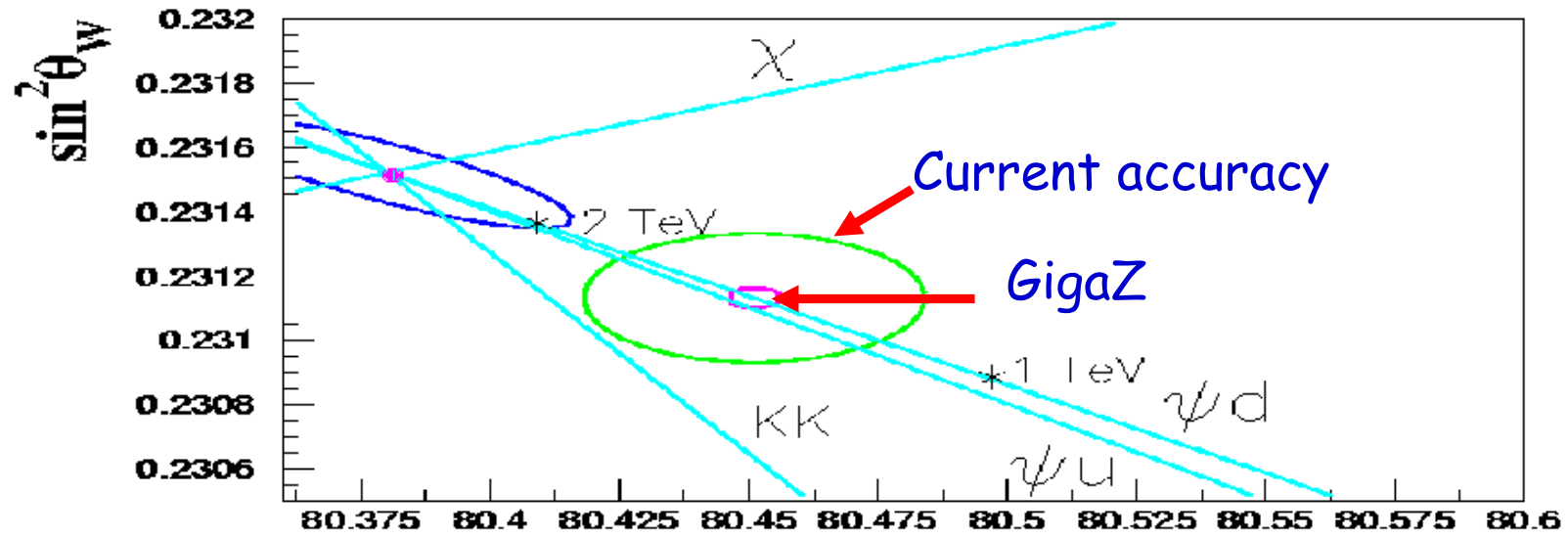


Discover of an extra gauge boson at the LHC  $\Rightarrow$  **measure the mass**

LC is sensitive to  $g/M_Z$ .  
 Mass at LHC + precision LC measurements allows to **determine the couplings** and distinguish between different scenarios

# Precision measurements

Assume no  $Z'$  etc. detected directly at the LHC  
 Revisit the Z with a Z- factory (Giga-Z:  $10^9$  Zs!)



Example interplay scenarios

$M_W$  GeV

Little Higgs: assume LHC sees Higgs at 300 GeV

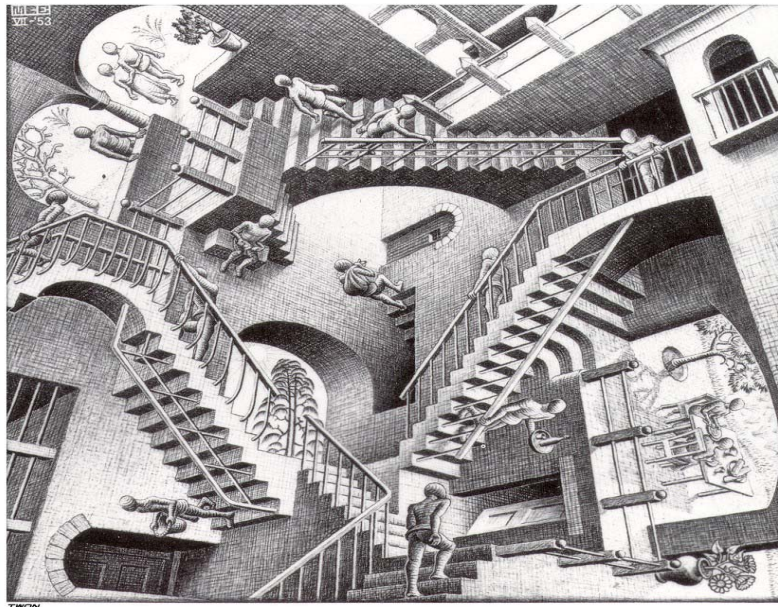
⇒ Giga-Z can estimate the mass of the  $Z'$  (U(1) singlet), say 5 GeV

Universal extra dimensions: assume LHC sees a light Higgs only.

⇒ Giga-Z demonstrates that direct and indirect Higgs mass meas. disagree

Improve search strategy or increase energy of LHC (a little)

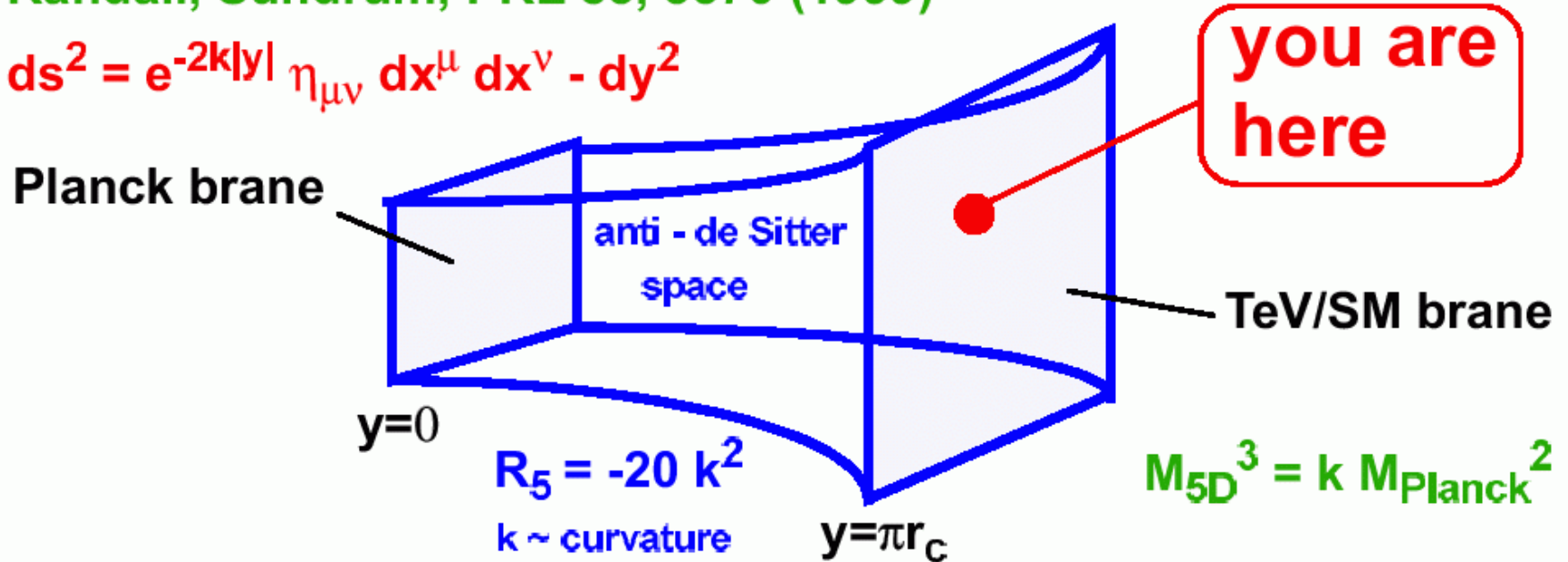
# 4. Extra Dimensions



# Curved Space: RS Extra Dimensions

Randall, Sundrum, PRL 83, 3370 (1999)

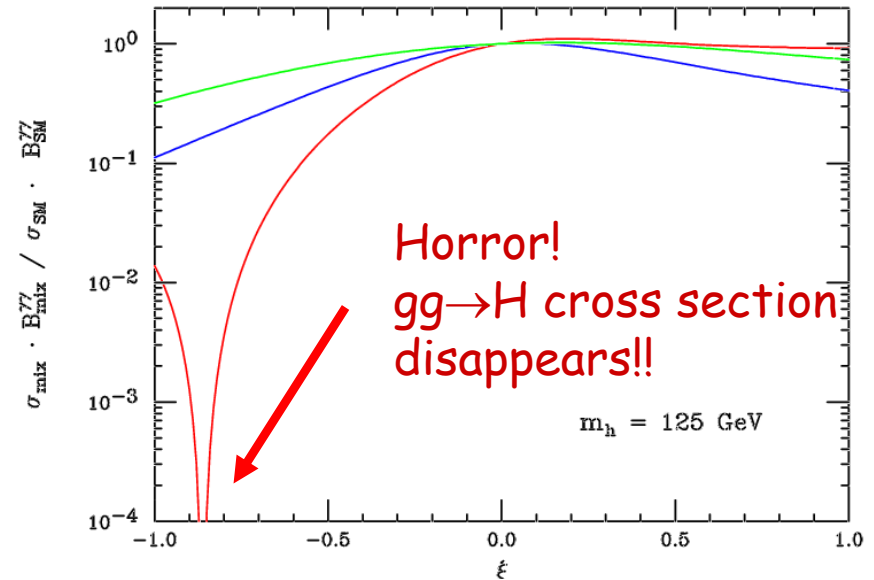
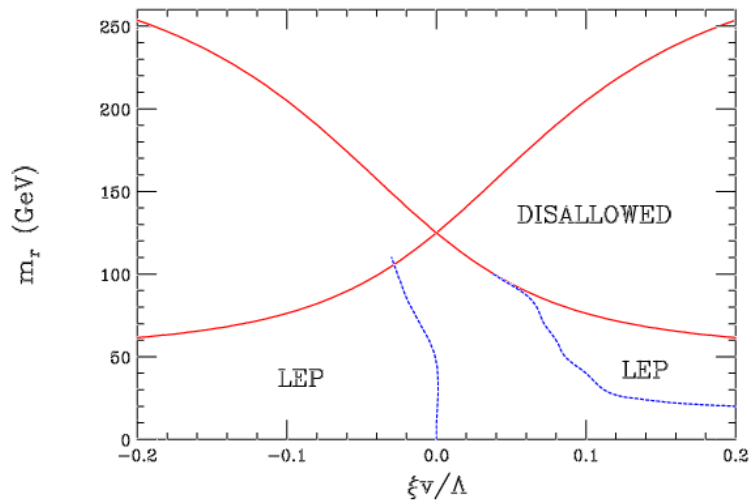
$$ds^2 = e^{-2k|y|} \eta_{\mu\nu} dx^\mu dx^\nu - dy^2$$



- Gravity strong at  $y=0$  and falls like  $\exp(-ky)$
- Gravity scale  $\Lambda_\pi = M_{\text{Planck}} \exp(-k\pi r_c) \sim \text{TeV}$  — no hierarchy
- Graviton resonances  $m_n = x_n k \exp(-k\pi r_c)$ ,  $J_1(x_n)=0$
- $M_{\text{Planck}}/M_{\text{electroweak}} \Rightarrow kr_c \sim 11-12$
- Newton's law  $\Rightarrow |R_5| < M_{5D}^2 \Rightarrow \text{coupling } c < 0.1$

# Radions!

- Models with 3-branes in extra dimensions predict radions
- Quantum excitations of brane distance in RS theories



- ✧ Radion Couplings to Gauge Bosons and Fermions similar to SM  $H^0$ ;
- ✧  $\phi$  Mixing to  $H$   $\xi$  cause shift in  $g_{HVV}$  and  $g_{Hff}$  couplings

Three Fundamental Parameters :

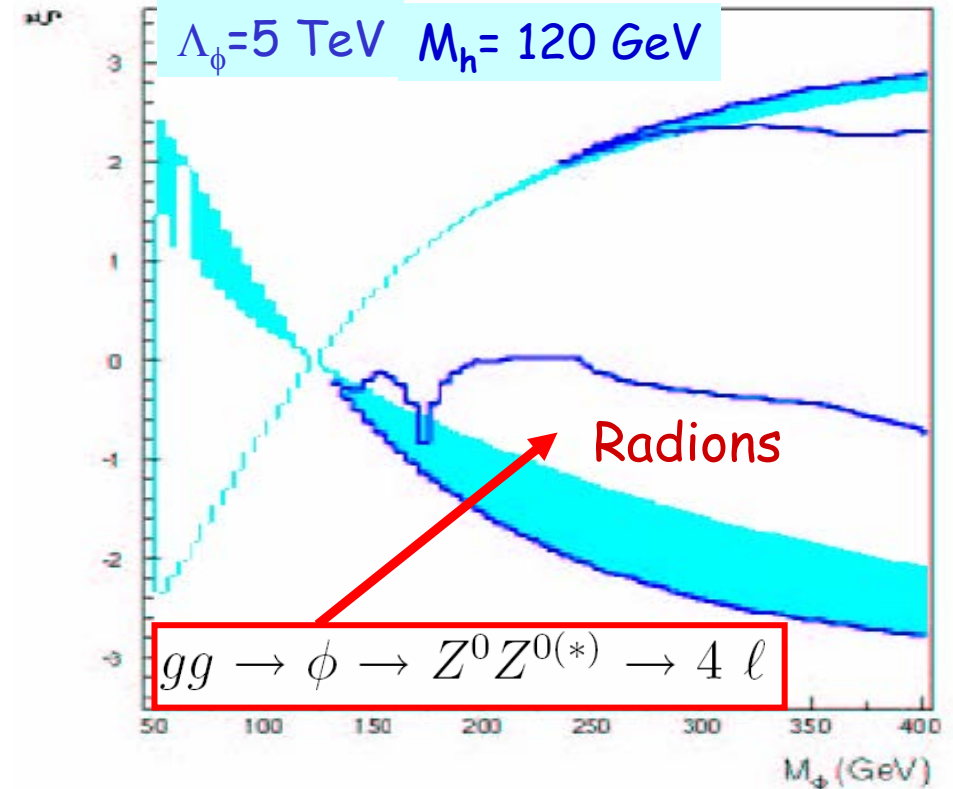
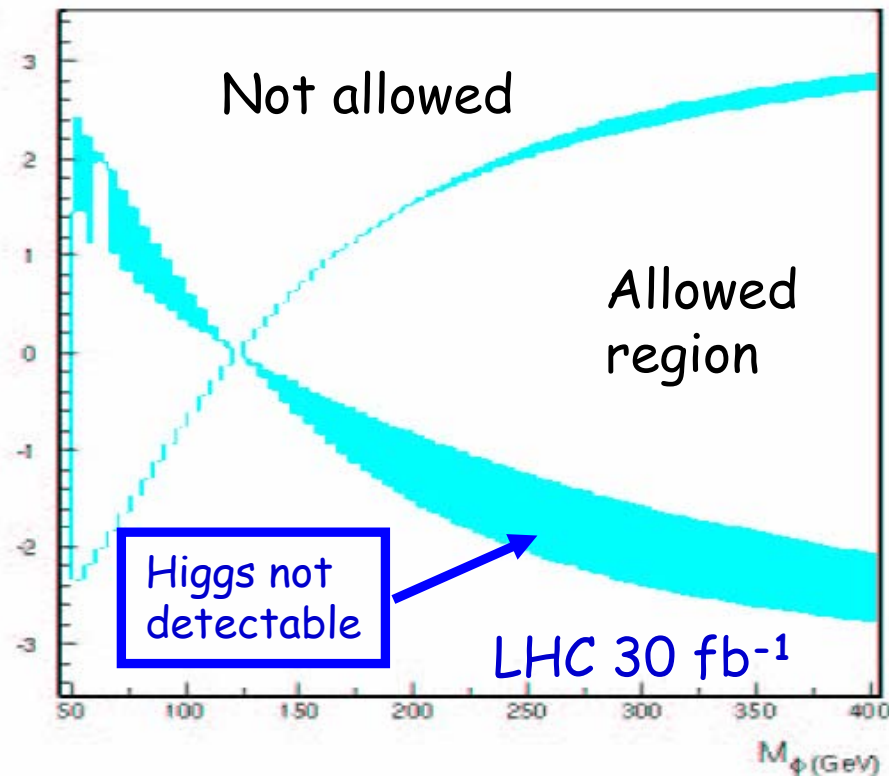
$$m_r \quad \xi \quad v/\Lambda$$

Can change things a lot for the LHC

# Higgs and Radion Searches

Battaglia, ADR, DeCurtis, Dominici, Gunion

Detectability at the LHC versus mixing  $\xi$  and mass of the radion  $M_\phi$



LHC has regions from the parameters space where it cannot find the Higgs  
However in most of these regions LHC will observe a Radion  
 $\Rightarrow$  LHC will essentially always see a scalar particle.

# Higgs or Radion?

- At LHC mostly ratios of couplings are determined
- Radions: same fermions/ $WW, ZZ$  coupling ratio as for SM Higgs
- Couplings to  $\gamma\gamma$  and  $gg$  receive anomalous contributions  $\rightarrow$  e.g.  $g_{H\gamma\gamma}/g_{HWW}$

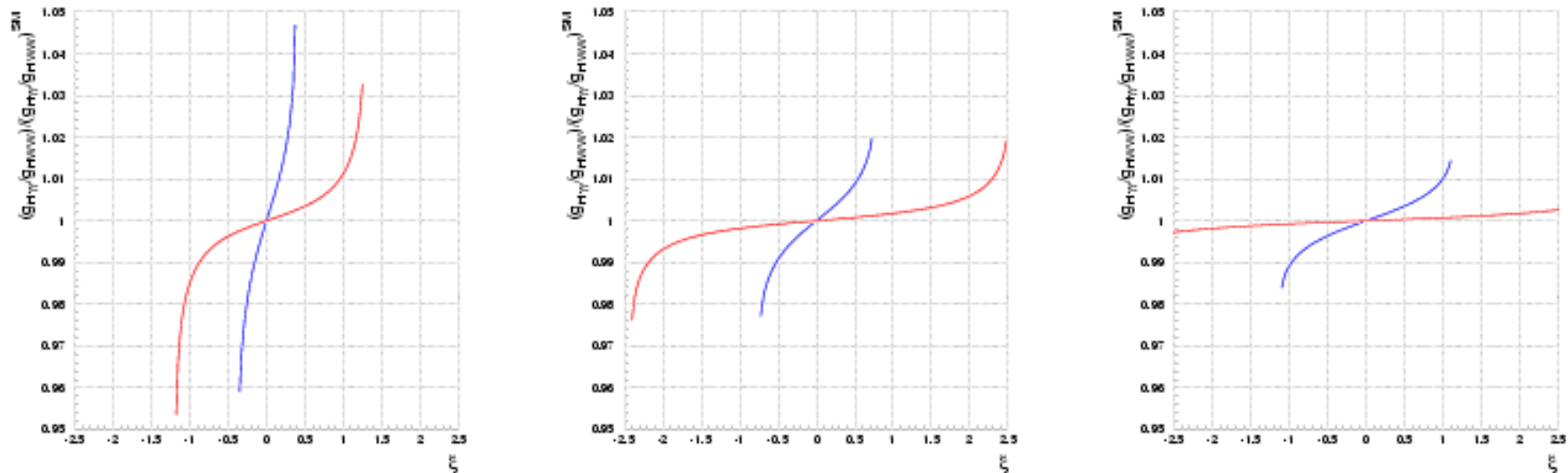


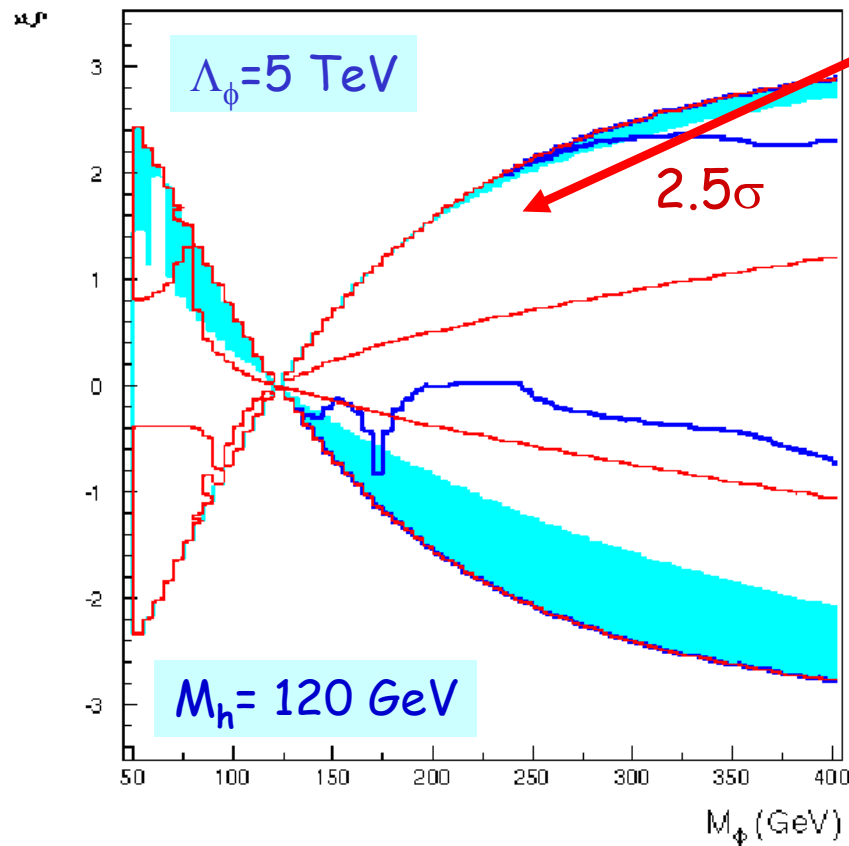
Figure 4: Ratio of couplings  $g_{H\gamma\gamma}^{effective}/g_{HWW}$  normalised to the SM prediction as function of  $\xi$ . Results are obtained for  $M_H=120$  GeV and  $\Lambda=2.5$  TeV (left), 5.0 TeV (center) and 7.5 TeV (right). The darker (blue) curves refer to  $M_\phi = 150$  GeV and the lighter (red) to  $M_\phi = 300$  GeV.

Effects are  $\sim 1-5\%$ : Difficult to establish at LHC

Some absolute rates go down up to factor 2 for  $m_\phi > 2m_h$  and  $\xi \neq 0$

# Radions @ a Linear Collider

- Nature ( $h$  or  $\phi$ ) can be determined at LC since it measures absolute coupling strengths with a few % accuracy: e.g. using couplings to  $bb$  and  $WW$



If mixing is strong enough the LC can easily distinguish a Higgs from a Radion

## ...more...

- Lots more on
  - Electroweak physics
  - QCD
  - Top physics
  - ADD extra dimensions
  - CP studies in the Higgs sector
  - Higgs potential
  - NMSSM studies
  - Little Higgs studies
  - 'Invisible' Higgs
  - Contact interactions
  - etc... etc.

# Summary

- Topics covered here just a small survey.

Expect the first document to be a basis for future work, summarize where we are and give guidance for future studies

- Several studies still need to be worked out quantitatively
- Certainly more ideas will come when we think a bit harder.

If you have any, please do join us.

- Combined information from LHC& LC better than the sum of both separately.

Not surprising, but quantified in coherent examples

- Need to Run the machines at the same time:

A few concrete examples studies.

- Impact of LC data on analyses strategy, luminosity/detector upgrades, triggering etc. at LHC started but needs more work

Ideas exist, e.g. stable gluinos in split SUSY, metastable Staus in models with gravitino LSP, decays of massive particles in many soft particles...

Positive outcome is good synergy between LHC and LC enthusiasts